

# Precise determination of the frequency of hyperfine splitting of muonium in quartz

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We have measured the frequency of hyperfine splitting  $\nu_0$  for a muonium atom impurity in quartz,  $\nu_0^{\text{SiO}_2} = 4438 \pm 8$  MHz. This value for  $\nu_0$  is negligibly different from the vacuum value  $\nu_0^0 = 4463$  MHz. The experiment is carried out in an applied magnetic field  $H = 400$  Oe using equipment with a time resolution  $\Delta t \approx 0.32$  nsec.

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A technique for determining the frequency of hyperfine splitting of muonium ( $\mu^+ e^-$ ) using two-frequency precession was proposed in Ref. 1. The frequency of hyperfine splitting  $\nu_0^{\text{SiO}_2}$  of muonium in quartz in a magnetic field  $H = 100$  Oe was determined in Ref. 2 with an accuracy of 1.7%. Further improvement in the accuracy

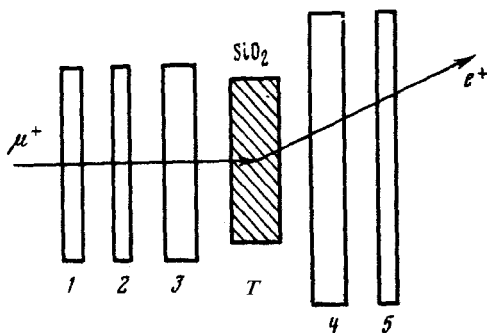


FIG. 1. Experimental setup.  $T$  is the quartz target, and 1-5 are the scintillators. Scintillator dimensions are: 1, 2- $100 \times 100 \times 10$  mm<sup>3</sup>; 3- $100 \times 100 \times 20$  mm<sup>3</sup>; 4- $150 \times 150 \times 20$  mm<sup>3</sup>; 5- $150 \times 150 \times 10$  mm<sup>3</sup>. The magnetic field  $H = 400$  Oe is perpendicular to the plane of the figure.

of determining  $\nu_0$  is possible by observing two-frequency precession in magnetic fields substantially greater than 100 Oe. However, observation of the Larmor precession of muonium  $\omega = eH/2m_e c$  ( $m_e$  is the electron mass) in fields  $H > 100$  Oe is difficult, since the precession period of muonium  $T = 2\pi/\omega$  becomes comparable to the time resolution  $\Delta t \approx 1.0$  nsec which is characteristic of the scintillation counters usually employed for the  $\mu^+ \rightarrow e^+$ -decay.<sup>3</sup>

The purpose of this work is to substantially improve the accuracy of determining  $\nu_0$ . In order to carry out this experiment special scintillation counters and recording apparatus were developed. The work was carried out on the Joint Institute for Nuclear Research (JINR) synchrocyclotron; a diagram of the experiment is given in Fig. 1. Signals from scintillation counter 1-5 were processed by the recording apparatus discussed in detail in Ref. 3. In order to increase the time resolution, the "opposed-photomultiplier" technique was used. This consisted of viewing scintillators 3 and 4 from two opposite sides with photomultipliers through light guides whose lengths were 20 cm for counter 3 and 60 cm for counter 4. Signals from the two photomultipliers, detecting a burst in scintillator 3, were fed into a "geometry compensation scheme"<sup>5</sup> whose output signal (the time  $t_\mu$  for the stopping of a  $\mu^+$ -meson in the target) is independent of the particle impact point in the scintillator. The signal  $t_e$  from counter 4 was generated in a similar manner, corresponding to the escape time of the  $\mu^+ \rightarrow e^+$ -decay positron from the target. The remaining scintillator were viewed by one photomultiplier each. Signals from these scintillators served for the logical selection of events. The time distribution  $t = t_e - t_\mu$  was analyzed by a time encoder with a differential nonlinearity of less than 1%. The integral nonlinearity of the encoder used was better than  $10^{-4}$ .<sup>6,7</sup> The time encoder channel value was measured with the help of a specially-developed scheme<sup>8</sup> with an accuracy better than  $10^{-4}$ . An encoder with a channel width of 0.10425 nsec was used in the experiment. The total number of channels was 4096. Using this apparatus we succeeded in obtaining a time resolution  $\Delta t \approx 0.32$  nsec, and in this way observing the two-frequency precession of muonium at  $H \approx 400$  Oe.

Let us consider the dependence of the polarization of the  $\mu^+$ -meson on time,  $P(t)$ , for muonium in an applied magnetic field. It is known that the function  $P(t)$  is described by the frequencies  $\nu_{ik}$  for transitions between muonium states with different quantum numbers<sup>1</sup>:

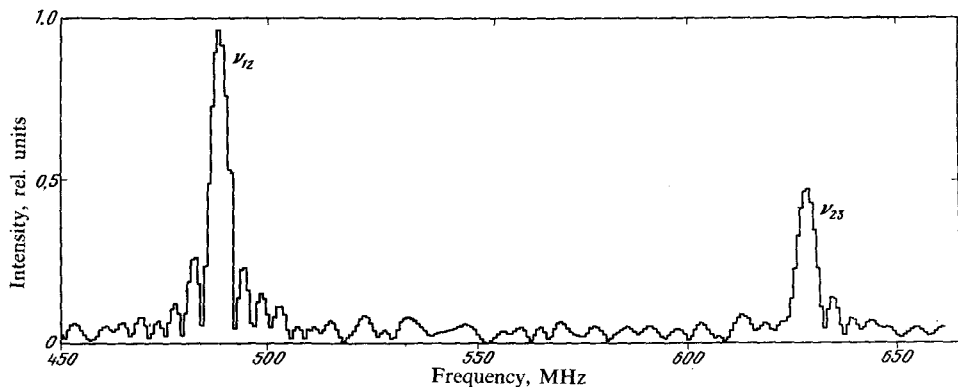


FIG. 2. Fourier transform of the experimental spectrum for  $\mu^+ \rightarrow e^+$ -decay in quartz in the field  $H = 400$  Oe.

$$\begin{aligned} \nu_{12} &= \frac{\nu_0}{2} + \nu_- - \delta, & \nu_{14} &= \frac{\nu_0}{2} + \nu_- + \delta, \\ \nu_{23} &= -\frac{\nu_0}{2} + \nu_- + \delta, & \nu_{34} &= \frac{\nu_0}{2} - \nu_- + \delta, \end{aligned} \quad (1)$$

where  $\delta = (\nu_0^2/4 + \nu_-^2)^{1/2}$ ,  $\nu_{\pm} = \nu(1 \pm \xi)$ , and  $\xi = m_e/m_\mu = 4.837 \times 10^{-3}$ , where  $m_\mu$  is the mass of the  $\mu^+$ -meson, and  $\nu = \omega/2\pi$ . For the case where the experimental time resolution does not allow the detection of the larger frequencies  $\nu_{14}$  and  $\nu_{34}$ , the dependence of the polarization  $P(t)$  of the  $\mu^+$ -meson on time in an applied field  $H < H_0 \approx 1590$  Oe ( $H_0$  is the hyperfine field at the muonium electron in the  $1S$ -state due to the magnetic moment of the  $\mu^+$ -meson) is written as<sup>1</sup>:

$$4P(t) = \left(1 + \frac{\nu_+}{\delta}\right) \cos 2\pi\nu_{12}t + \left(1 - \frac{\nu_+}{\delta}\right) \cos 2\pi\nu_{23}t. \quad (2)$$

The frequency of the hyperfine splitting  $\nu_0$ , according to Eq. (1), is expressed in terms of the observed frequencies  $\nu_{12}$  and  $\nu_{23}$ :

$$\nu_0 = \frac{2(\nu_{12} + \xi\nu_{23})(\nu_{23} + \xi\nu_{12})}{(\nu_{23} - \nu_{12})(1 - \xi)^2}. \quad (3)$$

The two-frequency precession of muonium was observed in our work in fused quartz in a field  $H = 400$  Oe. The experimental dependence  $N_{ex}(t)$  of the number of the escaping  $\mu^+ \rightarrow e^-$ -decay positrons in terms of beam momentum was described using a maximum probability technique by the expression

$$N(t) = N_0 e^{-t/\tau_0} [1 - \alpha e^{-\lambda t} P(t)], \quad (4)$$

where  $\tau_0 \approx 2.2 \times 10^{-6}$  is the  $\mu^+$ -meson lifetime,  $\alpha$  is the asymmetry coefficient for  $\mu^+$

$\rightarrow e^-$ -decay, and  $\lambda$  is the  $\mu^+$ -meson spin relaxation rate. In analyzing the experimental spectrum  $N_{\text{ex}}(t)$  in the interval  $t = 6\text{--}280$  nsec, the following values were obtained for  $\nu_{12}$  and  $\nu_{23}$ :

$$\nu_{12} = 487.08 \pm 0.07 \text{ MHz}, \quad \nu_{23} = 627.55 \pm 0.14 \text{ MHz}.$$

Figure 2 shows the Fourier transform of the resulting experimental spectrum  $N_{\text{ex}}(t)$ . From the experimental values for  $\nu_{12}$  and  $\nu_{23}$  and Eq. (3), it follows that the frequency of hyperfine splitting of the muonium atom in quartz is  $\nu_0^{\text{SiO}_2} = 4438 \pm 8$  MHz. It should be noted that exchange interactions between the muonium electron and electrons in the medium lead to a damping of the muonium precession and introduce a systematic error in the experimental value for  $\nu_0^{\text{SiO}_2}$ . In this experiment the relaxation rate is  $\lambda \approx 0.6 \mu\text{sec}$  which, according to Eq. (25) in Ref. 2, leads to a shift of  $\nu_0^{\text{SiO}_2}$  by an amount  $\Delta\nu/\nu \ll 10^{-4}$ .

Therefore, using this technique we succeeded in determining the value of  $\nu_0^{\text{SiO}_2}$  with an accuracy of 0.18%. The resulting value  $\nu_0^{\text{SiO}_2} = 4438 \pm 8$  MHz is three sigma less than the vacuum value  $\nu_0^0 = 4463$  MHz. This indicates that the interactions of the hydrogen-like atomic impurity (muonium) with the quartz lattice lead to an insignificant distortion of its electron structure. Since the Bohr radius of the atom in the 1S-state is  $r_0 \sim \nu_0^{-1/3}$  then, from the value  $\nu_0^{\text{SiO}_2} = 4438 \pm 8$  MHz, it follows that the Bohr radius of muonium in quartz is  $r_0^{\text{SiO}_2} = 1.0017 \pm 0.0006 r_0$ , where  $r_0 = 0.5 \text{ \AA}$  is the Bohr radius of the muonium atom in vacuum.

In conclusion, we note that the technique suggested for determining the frequency of the hyperfine splitting of the muonium atom in medium magnetic fields may be used successfully for a precise measurement of  $\nu_0$  for muonium in semiconductors.

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