

# Soft mode from the boundary of the Brillouin zone in the Raman-scattering spectrum of the paraphase of $\text{Hg}_2\text{Cl}_2$ and $\text{Hg}_2\text{Br}_2$

C. Barta,<sup>1)</sup> B. S. Zadokhin, A. A. Kaplyanskiĭ, and Yu. F. Markov

*A. F. Ioffe Physicotechnical Institute, USSR Academy of Sciences*

(Submitted August 6, 1977)

*Pis'ma Zh. Eksp. Teor. Fiz.* **26**, No. 6, 480–483 (20 September 1977)

Using the extrinsic ferroelastics  $\text{Hg}_2\text{Cl}_2$  and  $\text{Hg}_2\text{Br}_2$  as an example, we have observed, for the first time in phase transitions, the appearance of a soft mode from the boundary of the Brillouin zone (BZ) in the Raman scattering spectrum (RSS) of the paraphase ( $T > T_c$ ). The singularities of the RSS show it to be a first-order spectrum induced by structural disturbances of the lattice.

PACS numbers: 78.30.Gt, 61.50.Ks

In phase transitions in extrinsic ferroelectrics and ferroelastics, the actual soft mode corresponds to lattice vibrations with wave vector  $\mathbf{q}_{\text{max}}$  on the BZ boundary of the high-temperature ( $T > T_c$ ) paraphase. To observe this mode, neutron-scattering methods are used (see, e.g.,<sup>[1]</sup>). Observation of the mode from the BZ boundary in optical spectra of first order in the paraphase is forbidden by the selection rules with respect to the momentum  $\mathbf{q}$ , and is possible only in the ferrophase ( $T < T_c$ ) after the point  $\mathbf{q}_{\text{max}}$  is transferred to the center ( $\mathbf{q} = 0$ ) of the new BZ of the ferrophase.<sup>[2]</sup> In the present study we succeeded, for the first time, in observing the soft mode from the BZ boundary in the RSS in the *paraphase* at  $T > T_c$  (using the extrinsic ferroelastics  $\text{Hg}_2\text{Cl}_2$  and  $\text{Hg}_2\text{Br}_2$  as examples<sup>[3,4]</sup>). The behavior of the RSS favors the interpretation of this spectrum as being of first order and as being induced by static or dynamic disturbances of the regularity of the lattice.

The high-temperature phase  $\text{Hg}_2\text{X}_2$  ( $\text{X} = \text{Cl}, \text{Br}$ ) is tetragonal ( $D_{4h}^{17}$ ) and a structural transition into ferroelectric orthorhombic phase  $D_{4h}^{17}$  takes place after cooling to  $T_c = 185$  K ( $\text{Hg}_2\text{Cl}_2$ ) and  $T_c = 143$  K ( $\text{Hg}_2\text{Br}_2$ ). This transition was investigated mainly by the RSS method.<sup>[3,4]</sup>

In the present study, the RSS of single crystals of the tetragonal phase were investigated at a  $90^\circ$  scattering geometry in polarized light in a wide range of temperatures, from high ones  $\sim 400$  K (a limit imposed by the onset of sublimation of  $\text{Hg}_2\text{X}_2$ ) down to the phase-transition point  $T_c$ . The use of a triple monochromator ("Spex Ramalog") with an argon laser ( $\lambda = 4880$  Å,  $W = 500$  mW) made it possible to investigate in detail the RSS region near the exciting line. As a result, a weak ( $\sim 100$  times weaker than the fundamental RSS of the first order of the paraphase) low-frequency with a characteristic temperature dependence was observed in the RSS in the case of polarization in the "basal" plane  $xx$ ,  $yy$ , or  $xy$ .

Figure 1 shows the RSS of  $\text{Hg}_2\text{Cl}_2$  in the Stokes and anti-Stokes regions. A peak is observed at  $\Omega_{\text{SM}}$  with a frequency that decreases only as  $T \rightarrow T_c^+$ . We were able to trace a decrease of the frequency  $\Omega_{\text{SM}}$  from 14 to  $4.7$   $\text{cm}^{-1}$  (see Fig. 2b). In the temperature interval 265–195 K, the frequency squared behaves like  $\Omega_{\text{SM}}^2 \propto (T - T_c)$ . When the temperature is changed, the intensity decreases and the shape of the peak changes. In a certain intermediate temperature interval, a shoulder appears distinctly on the low-frequency slope of  $\Omega_{\text{SM}}$  (arrows on Fig. 1d), and attests to the presence of a second peak  $\Omega'$  in the RSS. All the indicated singularities were observed in the RSS of  $\text{Hg}_2\text{Br}_2$ , where the frequency  $\Omega_{\text{SM}}$  shifts from 12.4 to  $5.4$   $\text{cm}^{-1}$  when the temperature changes from  $T = 350$  K to  $T_c$ .

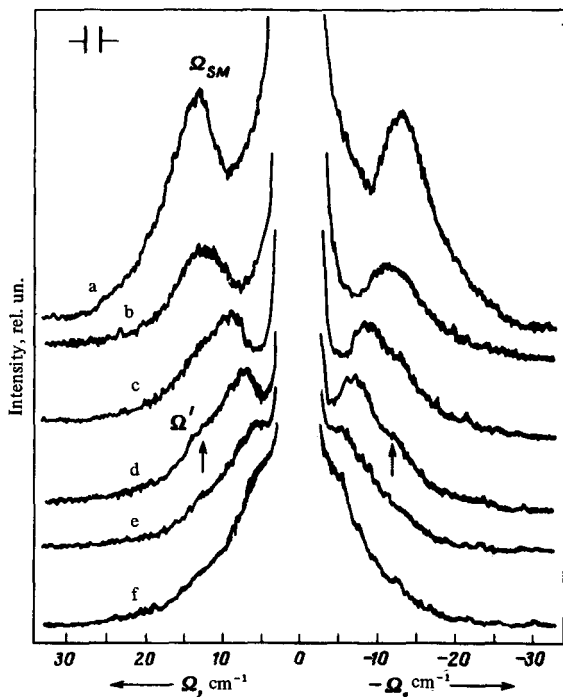


FIG. 1. Low-frequency RSS of  $\text{Hg}_2\text{Cl}_2$  at various temperatures: a— $T=327$  K, b— $T=294$  K, c— $T=274$  K, d— $T=221$  K, e— $T=210$  K, f— $T=202$  K.

The observed frequency shift  $\Omega_{SM} \rightarrow 0$  as  $T \rightarrow T_c^+$  points without doubt to a connection between  $\Omega_{SM}$  and the soft mode that induces the phase transition in  $\text{Hg}_2\text{X}_2$ . According to<sup>[3,4]</sup> this transition  $D_{4h}^{17} \rightarrow D_{2h}^{17}$  is due to condensation of the oscillation of the transverse acoustic branch  $\omega_{TA}(q)$  on the boundary of BZ of the paraphase at the  $X$  point of the BZ. It follows therefore that the  $\Omega_{SM}$  peak is connected with the oscillations at the  $X$  point of the BZ. The appearance of these oscillations in a first-order RSS can be due to disturbances in the regularity of the lattice. It is known<sup>[5]</sup> that violation of the translation symmetry of the lattice leads to violation of the selection rules with respect to  $q$  and makes it possible for oscillations with  $q$  in the entire BZ to appear in the spectrum; in this case, the maxima of the distribution in frequency  $g(\omega)$  appear in the (continuous) RSS.

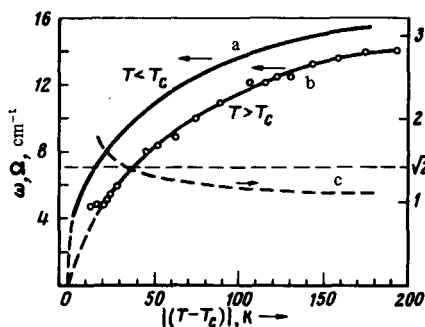


FIG. 2. Temperature dependence of the frequency of the soft mode at  $T < T_c$  (a) and  $T > T_c$  (b), and of the frequency ratio (c).

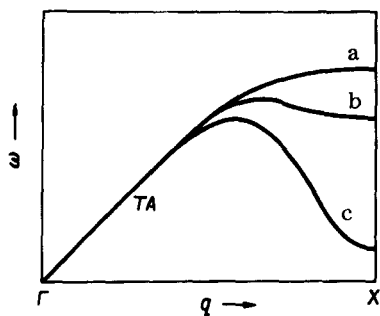


FIG. 3. Acoustic branch at different temperatures  $T(a) > T(b) > T(c)$  (scheme).

The quasi-continuous character of the observed RSS (its width is comparable with the frequency) confirms the connection between the spectrum and oscillations from different points of the BZ. We propose that the predominant contribution to the formation of the singularities (peaks) of the RSS and to their temperature dependence is made by oscillations of the transverse "soft-mode" acoustic branch  $\omega_{TA}(\mathbf{q}_{[111]})$  on the  $\Gamma-x$  line, which is the lowest acoustic branch (with the lowest speed of sound) of  $\text{Hg}_2\text{X}_2$ .<sup>[6]</sup> Figure 3 shows schematically the evolution of this branch as  $T \rightarrow T_c^+$ , when  $\omega_{TA}(X) \rightarrow 0$ . In the general case,  $\omega(\mathbf{q})$  has two extrema ( $\partial\omega/\partial\mathbf{q} = 0$ ) in which one can expect a maximum of the function  $g(\omega)$ . One of them is permanently at the point  $X$  with which the peak of the soft mode  $\Omega_{SM}$  in the RSS is connected. It is seen that as  $T \rightarrow T_c^+$  the minimum of  $\omega(\mathbf{q})$  near  $X$  "becomes deeper," and the gently sloping region near  $X$  where  $\partial\omega/\partial\mathbf{q} \approx 0$  [on which the amplitude of the maximum  $g(\omega)$  depends] becomes narrower. This can explain the decrease in the intensity of the  $\Omega_{SM}$  peak and its narrowing, which are observed in the RSS as  $T \rightarrow T_c^+$ . The second extremum of  $\omega(\mathbf{q})$  corresponds to the temperature-dependent maximum inside the zone (Figs. 3b and 3c). It is possible to attribute to it the band  $\Omega'$  observed in the RSS in a certain temperature interval. The existence of only one relatively narrow  $\Omega_{SM}$  peak in the RSS at high temperature (Fig. 1a) seems to indicate that the shape of  $\omega(\mathbf{q})$  is close to that of curve "a" (Fig. 3).

It is of interest to compare the behavior of the soft mode of  $\text{Hg}_2\text{X}_2$  in the paraphase at  $T > T_c$  with its behavior in the ferrophase at  $T < T_c$ , when this mode is allowed in the RSS because of the transfer of  $X$  to the center of the BZ of the ferrophase.<sup>[3,4]</sup> Figure 2a shows the temperature dependence of the frequency  $\Omega_{SM}(T)$  of the soft mode in the ferrophase of  $\text{Hg}_2\text{Cl}_2$  according to the data of<sup>[3]</sup>. It is seen that at a large distance from  $T_c$  the frequencies of the soft mode are close to each other in the para- and ferrophases. The same takes place also for  $\text{Hg}_2\text{Br}_2$ . The dashed curve in Fig. 2c shows the ratio  $\omega_{SM}/\Omega_{SM}$  of the frequencies of the soft mode in the ferrophase and paraphase at different  $|T - T_c|$ .

In a certain temperature region, this ratio is close to the value  $\sqrt{2}$  that follows from Landau's phenomenological theory [see formula (25) of<sup>[4]</sup>].

The proposed connection between the RSS and the first-order spectrum thus explains the principal experimental relations. The assumption that the observed RSS is connected with a second-order spectrum leads to excessively low values of the frequencies  $\omega_{TA}(X)$  of the paraphase of  $\text{Hg}_2\text{X}_2$ , which agreed poorly with the acoustic-measurement results<sup>[6]</sup> and with the RSS of  $\text{Hg}_2\text{X}_2$ .<sup>[3,4]</sup> The nature of the  $\text{Hg}_2\text{X}_2$  lattice disturbances that induce the RSS of first order remain unclear. Their concentration can be quite low, since the frequency  $\omega_{TA}(X)$  is apparently very "sensitive" to factors that lift the forbiddenness in  $q$ . This is seen from the anomalously strong peak of the soft-mode line  $\omega_{SM}$  in the RSS of the ferrophase.<sup>[3,4]</sup> It is probable that the disturbance is of thermal structural character, either static<sup>[7]</sup> or dynamic, and can be responsible for part of the temperature-dependent decrease of the RSS intensity as  $T \rightarrow T_c^+$ .

The authors thank I.I. Novak and V.V. Baptizanskiĭ for making it possible to measure the spectra and B.Z. Malkin and A.A. Klochikhin for a discussion.

<sup>1)</sup>Institute of Solid State Physics, Czechoslovak Academy of Sciences, Prague.

---

<sup>1</sup>G. Shirane and Y. Yamada, *Phys. Rev.* **177**, 858 (1969).

<sup>2</sup>P.A. Fleury, J.F. Scott, and J.M. Worlock, *Phys. Rev. Lett.* **21**, 16 (1968).

<sup>3</sup>C. Barta, A.A. Kaplyanskiĭ, V.V. Kulakov, and Yu.F. Markov, *Pis'ma Zh. Eksp. Teor. Fiz.* **21**, 121 (1975) [*JETP Lett.* **21**, 54 (1975)]; *Solid State Commun.* **21**, 1023 (1977).

<sup>4</sup>C. Barta, A.A. Kaplyanskiĭ, V.V. Kulakov, B.Z. Malkin, and Yu.F. Markov, *Zh. Eksp. Teor. Fiz.* **70**, 1429 (1976) [*Sov. Phys. JETP* **43**, 744 (1976)].

<sup>5</sup>A.A. Maradudin, *Solid State Phys.* **18**, 273 (1966); **19**, 1 (1966).

<sup>6</sup>I.M. Sil'vestrova, C. Barta, G.F. Dobrzanskiĭ, L.M. Belyaev, and Yu.V. Pisarevskii, *Kristallografiya* **20**, 359 (1975) [*Sov. Phys. Crystallogr.* **20**, 221 (1975)].

<sup>7</sup>T.I. Maksimova, A.I. Stekhanov, and E.V. Chisler, *Fiz. Tverd. Tela* **7**, 1881 (1965) [*Sov. Phys. Solid State* **7**, 1515 (1965)].