

Electroexcitation of giant multiple resonances in ^{64}Zn and ^{124}Sn nuclei

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Results are presented of the investigation of giant multiple resonances in the nuclei ^{64}Zn and ^{124}Sn with the aid of inelastic scattering of electrons, performed in Khar'kov with the LUÉ-300 linear electron accelerator.

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To obtain information on the region of the giant resonance, the initial spectrum was first corrected for the radiative elastic-scattering effects, and next for radiative and ionization losses at each point of the remaining spectrum. For the ^{64}Zn nucleus we subtract also the contribution of the discrete levels with excitation energies from 0.99 to 10.6 MeV, which were determined in^[1,2]. No

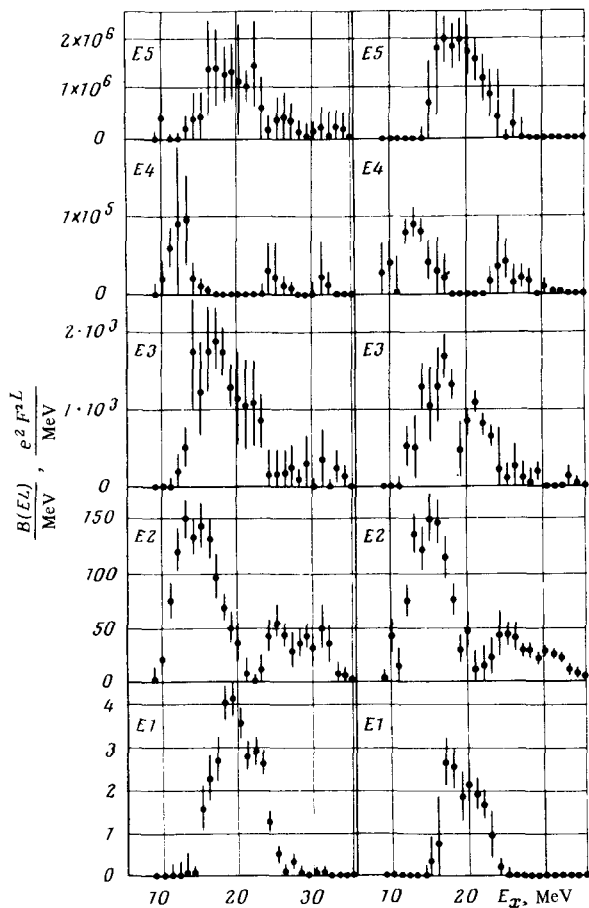


FIG. 1. ^{64}Zn . Dependence of the relative probabilities of transitions with multiplicities $L=1-5$ on the excitation energies. Left—Helm's model, right—high-energy approximation.

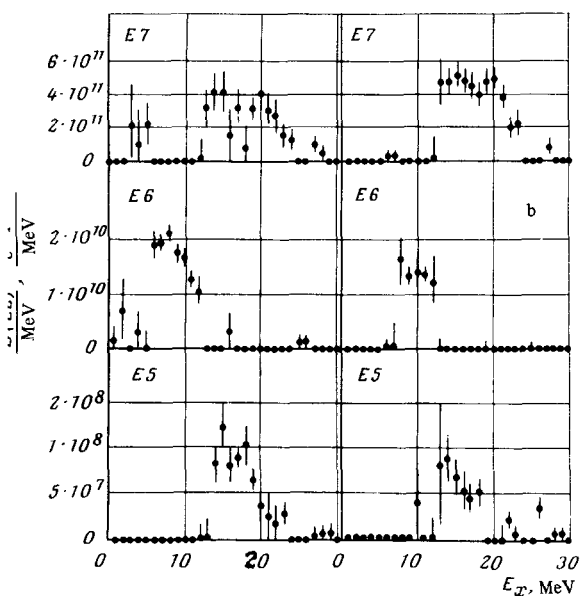
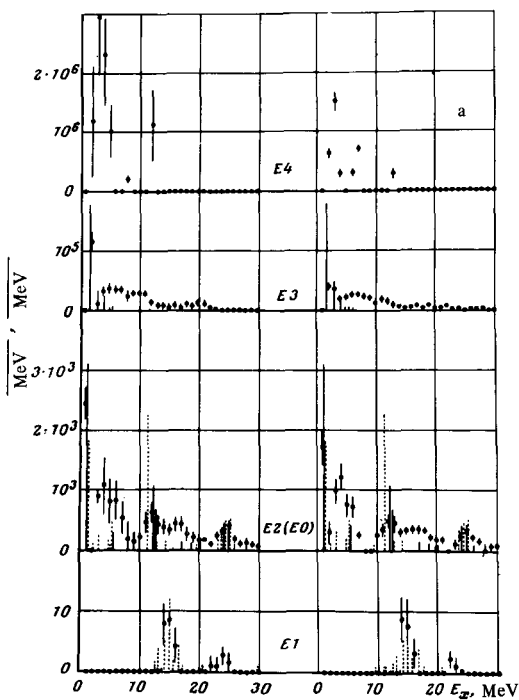
such subtraction was carried for ^{124}Sn . The contribution of a quasielastic scattering cross section was estimated by us on the assumption that this cross section is described within the framework of the single-particle cell model with allowance for the distortion of the electron and proton waves. The calculated curve was normalized to the point of the spectrum in the excitation-energy region $E_x \sim 35$ MeV.

After subtracting quasielastic scattering cross sections we carried out a multiple analysis of the remaining parts of the spectra. To this end, the spectra was broken up into bands 1 MeV wide and the form factor of each band was obtained. The form factor of each band was then represented as a sum of five multiple form factors for ^{64}Zn and seven form factors for ^{124}Sn ,

$$F^2 = \sum_{L=1}^N \beta_L F_{EL}^2$$

where β_L are fit parameters, and the multiple form factors are taken from Helm's model and from the high-energy approximation.

The parameters of the charge distribution in the ground state, used in the calculations, are given in Table I.



G. 2. ^{124}Sn . Dependence of the relative probabilities of the transitions of multipolarities $L=1-4$ (a) and $L=5-7$ (b) on the excitation energy. Left—Helm's model, right—high-energy approximation.

TABLE I.

Nucleus	R, F	G, F	c, F	β, F
^{64}Zn	4.5 [4]	0.921 [4]	4.183 [6]	0.603 [6]
^{124}Sn	5.78 [5]	1.264 [5]	5.490 [6]	0.534 [6]

This fit made it possible to separate the excitations with different multipolarities L , and knowledge of the dependence of β_L on E_x has made it possible to plot the E_x -dependence of t relative probabilities of the transitions $B(EL)$.

TABLE II.

 ^{64}Zn

EL	E_x, MeV	Γ_x, MeV	$B(EL), e^2 F^2 L$	ΔT	Lim. of EWSR, %		$E_x A^{2/3} / \text{MeV}$		
					total	$\Delta T = 0.1$	our data	others	
E1	17.7 ± 0.6	4.3 ± 0.8	9.5 ± 2.1	1	-	63 ± 16	71 ± 3	78-82	
	21.4 ± 0.6	3.5 ± 0.8	4.5 ± 1.2	-	-	40 ± 11	86 ± 3		
E2	0-11	-	1380 ± 90	0	-	10 ± 1	-	58-65	
	15.0 ± 0.2	6.0 ± 0.4	600 ± 70	-	-	4.7 ± 0.5	-		
				0	-	49 ± 6	60 ± 1		
	25.1 ± 0.7	3.7 ± 1.6	90 ± 50	-	-	23 ± 3	-		100 ± 4
				1	-	11 ± 6	-		
30.4 ± 0.8	5.0 ± 1.7	110 ± 50	-	-	6 ± 3	-	121 ± 3	$411-140$	
E3	0-11	-	44100 ± 1200	0	-	18 ± 2	-	70-82	
	16.6 ± 0.4	4.2 ± 1.4	8500 ± 1800	-	-	8.6 ± 0.8	-		
				1	-	5.5 ± 1.2	66 ± 2		
21.4 ± 2.6	6.5 ± 3.1	6500 ± 2200	-	-	5.4 ± 2.0	-	86 ± 10	$105-158$	
E4	0-11	-	$(1.3 \pm 0.2) \times 10^5$	-	-	4.0 ± 0.2	-	52±2	
	12.9 ± 0.5	3.2 ± 1.1	$(2.8 \pm 1.2) \times 10^5$	-	-	2.0 ± 1.2	-		
E5	25.4 ± 0.8	2.5 ± 1.4	$(4.4 \pm 2.5) \times 10^4$	-	-	0.7 ± 0.3	-	102 ± 4	
	0-35	-	$(1.0 \pm 0.5) \times 10^6$	-	-	2.0 ± 1.0	-		

 ^{124}Sn

E1	14.8 ± 0.3	2.3 ± 0.5	20.8 ± 8.0	1	-	69 ± 26	74 ± 2	78-82	
	23.8 ± 0.9	2.5 ± 1.1	4.6 ± 3.4	-	-	25 ± 18	119 ± 5		
E2	0-8	-	6800 ± 870	0	-	54 ± 3	-	58-65	
	11.7 ± 0.5	3.0 ± 1.0	1580 ± 880	-	-	22 ± 2	-		
				0	-	50 ± 28	58 ± 3		
	24.9 ± 0.2	3.2 ± 0.5	1300 ± 260	-	-	20 ± 11	-		124 ± 1
1				-	36 ± 7	$411-140$			
E0	16.5 ± 1.0	6.4 ± 1.8	2400 ± 1100	-	-	44 ± 12	-	58-82	
	-	-	1490 ± 700	0	-	54 ± 25	82 ± 5		
E3	0-8	-	$(22.0 \pm 2.1) \times 10^4$	0	-	17 ± 3	-	70-82	
	10.8 ± 0.3	4.0 ± 0.6	$(6.7 \pm 1.3) \times 10^4$	-	-	42 ± 7	54 ± 2		
E4	18.9 ± 0.5	6.3 ± 1.2	$(5.2 \pm 1.2) \times 10^4$	-	-	8 ± 2	-	94 ± 3	$105-158$
	0-30	-	$(6.3 \pm 1.2) \times 10^5$	-	-	13 ± 3	-		
E5	0-30	-	$(6.0 \pm 1.8) \times 10^8$	-	-	5 ± 1	-		
E6	0-30	-	$(1.0 \pm 0.2) \times 10^{11}$	-	-	19 ± 6	-		
E7	0-30	-	$(4.3 \pm 0.8) \times 10^{18}$	-	-	21 ± 3	-		
						18 ± 4	-		

Figure 1 shows the dependence of the relative transition probabilities on the excitation energy for ^{64}Zn . The same dependence for ^{124}Sn is shown on Figs. 2(a) and 2(b).

Figure 2(a) shows the results of the theoretical calculations for E1 and E2 excitations within the framework of the theory of finite Fermi systems (dotted lines)^[7] and for E2 and E3 excitations in the random-phase approximation method^[8] (solid lines). Calculations of the E1 excitations were carried out for ^{124}Sn , and of E2 and E3 excitations for ^{120}Sn , since there are no such published calculations for ^{124}Sn . Nor are there theoretical calculations of the values of the EL excitations for ^{124}Sn . The calculations of the E3 excitations were carried out for $E_x=0-10$ MeV.

The presence of resonances above the particle-emission threshold has made it possible to divide the resolved excitations into individual sections. For the E1, E2, E3, and E4 excitations the cross section in this region was represented as a combination of two or three Gaussians, with parameters E_x , Γ_x , and $B(\text{EL})$ fitted by least squares to the experimental points. This fitting has made it possible to determine, with fair accuracy, the energy position, the half-widths, and the relative probabilities of the transitions and of the coverage of the energy-weighted sum rules (WISR) for giant multiple resonances. The averaged value of the fit in accordance with the two models is shown in Table II. The values of $\langle r^2 \rangle$ and $\langle r^{2L-2} \rangle$ were taken from the elastic-scattering data.^[6]

An examination of the E1—E3 resonances shows that the positions of the resonances agree well with the results of calculations in accordance with the dynamic collective model,^[9] in accordance with the random-phase approximation,^[8,10] and by the method of finite Fermi systems,^[7] as well as with calculations based on the sum rule.^[9] The results of these calculations are given in the 4th column of the table.

V.A. Nemashkalo, V.P. Likhachev *et al.*, in: *Voprosy atomnoy nauki i tekhniki (Problems of Atomic Science and Technology)*, Ser: *Fizika vysokikh energii i atomnogo yadra (High-Energy and Atomic Physics)*, No. 1 (17), Khar'kov, FTI Akad. Nauk Ukr. SSR 38, 1976.

V.A. Nemashkalo, V.P. Likhachev *et al.*, *ibid*, No. 2 (19), 62, 1977.

J. Klawansky, H.W. Kendall, A.K. Kerman, and D.B. Isabelle, *Phys. Rev. C* 7, 795 (1973).

V.D. Afanas'ev, N.G. Afanas'ev *et al.*, *Yad. Fiz.* 12, 885 (1970) [*Sov. J. Nucl. Phys.* 12, 480 (1971)].

J. Barrean and J.B. Bellicard, *Phys. Lett.* 25B, 470 (1967).

V.S. Litvinenko *et al.*, *Yad. Fiz.* 14, 479 (1971) [*Sov. J. Nucl. Phys.* 14, 269 (1972)].

N. Borzov and S.P. Kamerzhiev, Preprint FEI-580, Obninsk, 1975.

V.G. Soloviev, Ch. Stoyanov, and A.J. Vdovin, Preprint E4-10397, Dubna, 1977.

J. Bergere, *Elektromagnitnye vzaimodeystviya yader pri malykh i srednikh energiyakh (Electromagnetic Interactions of Nuclei at Low and Medium Energies)*, Proc. Third Seminar, Moscow, Nauka, 3, 1976.

V.F. Semenko, Preprint FIAN SSSR No. 72, Moscow, 1976.