

M. Lifshitz phase transitions in the n -type alloy $\text{Bi}_{0.924}\text{Sb}_{0.076}$ under tension

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A new method of producing strong elastic tensile strains ($\sim 1\%$) in the n -type alloy $\text{Bi}_{0.924}\text{Sb}_{0.076}$ used to observe the transition from a three-ellipsoid to a single-ellipsoid Fermi surface when stretched along the binary axis and to a two-ellipsoid surface when stretched along the bisector axis.

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The Lifshitz phase transitions,^[1] which are accompanied by a qualitative change in the topology of the Fermi surface, were observed under hydrostatic compression in a large number of substances. In the case of uniaxial deformations, owing to the low elastic limit of most metals and the impossibility of producing sufficiently strong deformations, a change in the topology of the Fermi surface was observed only for Zn whiskers^[2] at 0.35% elongation. Recently developed methods of obtaining strong elastic compression strains^[3,4] and tension strains,^[5] reaching 1% in alk crystals, greatly extend the possibilities of investigating the I.M. Lifshitz phase transitions under uniaxial deformations.

A detailed investigation of the energy spectrum of Bi under compression^[6,7] and tension^[5,6,8] by these methods has shown that if the strains are perpendicular to the crystal trigonal axis the electronic extrema at the points L of phase space are no longer equivalent, so that the electron

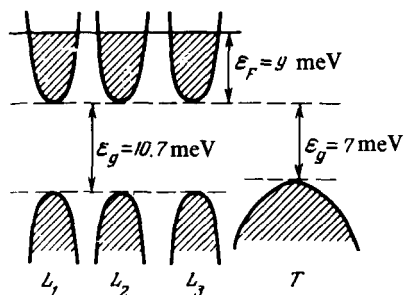


FIG. 1. Arrangement of the electron and hole extrema of n -type $\text{Bi}_{0.924}\text{Sb}_{0.076}$ near the Fermi level.

"ellipsoids" of the Fermi surface of Bi vary in different manners with changing load: the volume of one of the ellipsoids increases and that of the two others decreases in the case of compression along the bisector axis C_1 and tension along the binary axis C_2 , whereas two ellipsoids increase and one decreases if the tension is along C_1 and the compression along C_2 . It is obvious that in the case of sufficiently strong deformations ($\geq 1\%$ [5,7]) in these directions a qualitative change should take place in the Fermi surface of Bi, which should turn into a single ellipsoid in the former case and into two ellipsoids in the latter.

Inasmuch the deformations needed to observe the expected phase transition of Bi exceed 1% the object of the investigation was chosen to be the alloy $\text{Bi}_{0.924}\text{Sb}_{0.076}$ doped with $10^{-4}\%$ of Te, in which the Fermi energy of the electrons is much lower than that of Bi. The main characteristics of the energy spectrum of this alloy [9,10] are shown in Fig. 1. The small Te additive to this alloy leads to a filling of the electronic extrema in L . The presence of a sufficiently large gap between the extrema in L and T gives grounds for expecting the total number of the electrons to remain unchanged after the deformation, and that the change of the volumes of the ellipsoids is due exclusively to the transfer of carriers from some extrema (no longer equivalent) L_i to others.

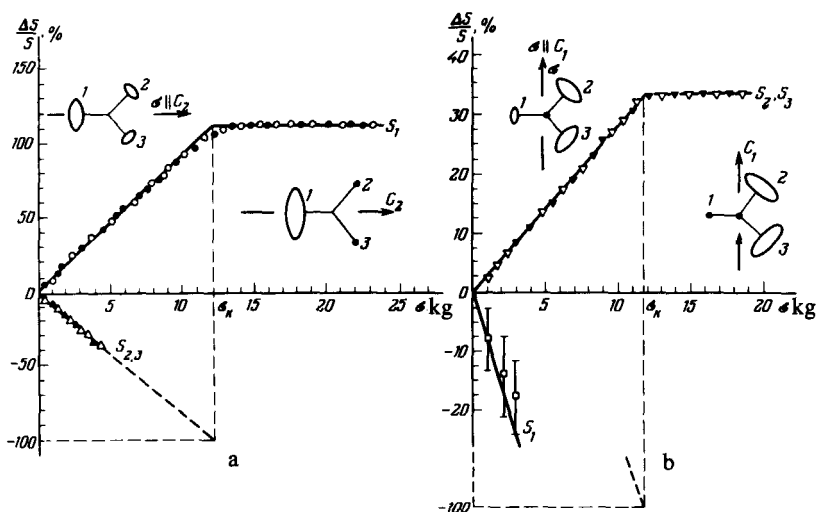


FIG. 2. Dependence of the extremal sections of the Fermi surface of n -type $\text{Bi}_{0.924}\text{Sb}_{0.076}$ on the load at $\sigma \parallel C_2$ (a) and $\sigma \parallel C_1$ (b): sample 1: \circ — $-85^\circ \leq \phi \leq 0^\circ$, Δ — $0^\circ \leq \phi \leq 10^\circ$, sample 2: \circ — $-85^\circ \leq \phi \leq 0^\circ$, Δ — $0^\circ \leq \phi \leq 10^\circ$, sample 3: Δ — $-10^\circ \leq \phi \leq 10^\circ$, $80^\circ \leq \phi \leq 100^\circ$, \circ — $H \parallel C_2$, sample 4: Δ — $-10^\circ \leq \phi \leq 10^\circ$, $80^\circ \leq \phi \leq 100^\circ$.

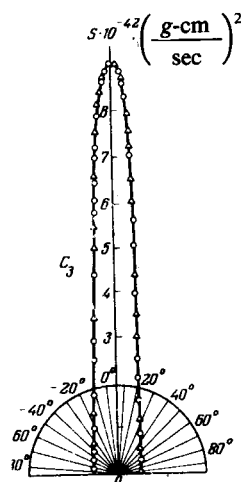


FIG. 3. Angular dependence of the extremal sections in the trigonal-bisector plane for the single-ellipsoid Fermi surface of the n -type alloy $\text{Bi}_{0.924}\text{Sb}_{0.076}$ at $12.5 \text{ kg} < \sigma < 25 \text{ kg}$: \circ —sample 1, Δ —sample 2. Solid line—ellipse drawn through the extremal sections.

Since direct observation of the vanishing of the individual parts of the Fermi surface under deformation with the aid of the Shubnikov-de Haas effect is impossible, owing to the sharp decrease of the oscillations from the decreasing groups of carriers, the I.M. Lifshitz phase transitions that are accompanied by topological changes of this kind are more conveniently detected by the accompanying change of the rate of increase of the other parts of the Fermi surface. From this point of view, the n -type alloy $\text{Bi}_{0.924}\text{Sb}_{0.076}$ is a more convenient object for a distinct observation of the expected phase transition than pure Bi, in which the vanishing of individual electronic extrema takes place against the background of varying overlaps of the bands in L and T .

The samples were stretched in the apparatus described in^[5] in the direction of the binary or bisector axis, up to a strain $\epsilon_{xx} \sim 0.6\%$ in the tension direction and $\epsilon_{yy} \sim 0.4\%$ in the perpendicular direction. The strains were determined at room temperature with the aid of FKPA-1 small-base oil strain resistors and amounted to $\epsilon_{xx} \approx 0.025\% \text{ kg}^{-1}$ and $\epsilon_{yy} \approx -0.15\% \text{ kg}^{-1}$. The change of the energy spectrum under tension was investigated with the aid of the Shubnikov-de Haas effect by the usual modulation method in the temperature interval 1.9–4.2 K and in magnetic fields up to 45 Oe at loads up to 23 kg.

The dependences of the extremal sections of the Fermi surface on the values of σ were investigated in a wide range of angles ϕ with the magnetic field oriented in the trigonal-bisector plane ($\sigma \parallel C_2$) and trigonal-binary ($\sigma \parallel C_1$) planes. ϕ was reckoned from the trigonal axis C_3 of the sample. The measurements were made on four different samples. All the observed cross sections of each ellipsoids vary with load in like fashion as shown in Fig. 2. The figures show also the schematic arrangement of the electron ellipsoids of the Fermi surface in the basal plane and indicates the character of their variation in the course of dilatation.

It is obvious that the increase of ellipsoid 1 in the case $\sigma \parallel C_2$ and of ellipsoids 2 and 3 at $\sigma \parallel C_1$ continues until the electronic extrema of L_p , which correspond to decreasing ellipsoids, rise above the Fermi level. At that instant, at $\sigma_k = 12 \pm 0.3 \text{ kg}$, it follows from Figs. 2a and 2b that in both cases the decreasing ellipsoids vanish, and the increase of the remaining ellipsoids ceases because the influx of the carriers is stopped. Thus, in the n -type alloy $\text{Bi}_{0.924}\text{Sb}_{0.076}$ at values $\sigma_k \parallel C_2$ ($\epsilon_{xx} \approx 0.3\%$; $\epsilon_{yy} \approx -0.2\%$) an electronic phase transition takes place from a three-ellipsoid to a single-ellipsoid equal-energy surface, and at $\sigma_k \parallel C_1$ a transition takes place from three-ellipsoid to a two-ellipsoid surface (Figs. 2a and 2b).

It should be noted that the amplitudes of the oscillations of the magnetoresistance due to the increasing parts of the Fermi surface increases to $\sigma \sim \sigma_k$, after which it remains constant. The maximum changes of the volumes of the ellipsoids, namely $V_\sigma/V_0 \approx 3$ when the single-ellipsoid surface is produced and $V_\sigma/V_0 \approx 1.5$ when a two-ellipsoid surface is produced, indicate that all the existing carriers are transferred to the electronic extrema that remain below the Fermi level.

By obtaining a single-ellipsoid Fermi surface we were able to determine its parameters with high accuracy. For the obtained single-ellipsoid surface, oscillations of the magnetoresistance are observed at all directions of the magnetic field in the trigonal-bisector plane. This has made it possible to determine directly, for the first time ever, the principal intersections of the Fermi surface with this plane: $S_{\min} = (0.52 \pm 0.02) \times 10^{-42} \text{ (g cm/sec)}^2$ and $S_{\text{int}} = (9.0 \pm 0.2) \times 10^{-42} \text{ (g cm/sec)}^2$ (Fig. 3). The cyclotron effective masses on the principal sections are $m^*/m_0 = 0.092 \pm 0.004$ and $m^*_{\min}/m_0 = 0.0059 \pm 0.0006$. The mass anisotropy is $m^*_{\text{int}}/m_0 = 15$, somewhat less than the section anisotropy $S_{\text{int}}/S_0 = 17.3$.

The Dingle temperature determined at $\sigma = 16 \text{ kg}$ amounts to $T_D = (2.2 \pm 0.3) \text{ K}$, thus pointing to a high degree of homogeneity of the strain in the investigated part of the sample.

The investigation of the Shubnikov oscillations in the trigonal-bisector plane in the direction $\phi = 1.5 \pm 0.5^\circ$ and $\phi = 8 \pm 0.5^\circ$ have revealed for the first time in Bi and in $\text{Bi}_{1-x}\text{Sb}_x$ alloys a spin damping (doubling of the frequency) in this plane.

In conclusion, we are sincerely grateful to Ya.G. Ponomarev for supplying the data on the structure of the spectrum of the investigated alloy.

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