

Effect of quasilinear effects on the propagation and damping of lower-hybrid waves in a plasma

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The quasilinear mechanism of “trapping” of the lower-hybrid waves on the periphery of a plasma is considered.

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A strange regularity was observed in all the experiments performed to date on additional heating of a plasma by lower-hybrid waves ($\omega^2 \gg \omega_{\text{LH}}^2 = \omega_{\text{pe}}^2 \omega_B \omega_{B_e} / (\omega_{\text{pe}}^2 + \omega_B \omega_{B_e})$, $|k_z c / \omega| > 1$, $k_z \parallel H_0$ in installations of the tokamak type.^[1] Despite the high efficiency ($\geq 90\%$) of RF energy input into the plasma, absorption of the energy by the long-lived plasma component was very small, not more than 20% of the energy input. The greater part of the RF energy vanished “without trace,” without increasing the energy content of the plasma. Generally speaking, this anomaly could be attributed to the nonlinear process of conversion of the lower-hybrid waves into short-wave plasma oscillations^[2]; if the characteristic length of energy transfer turns out to be much shorter than the plasma dimensions, then the RF energy dissipation should occur mainly on the periphery of the plasma. In most experiments, however, it was noted that at a moderate ($P < 100$ kW) energy input the intensity of the scattered waves decreased rapidly with decreasing plasma density; on the other hand, the heating efficiency was not increased thereby. The absence of nonlinear processes in discharges with $\omega > \omega_{\text{LH}}^{\text{max}}$ was attributed in a number papers^[3] to convective emergence of the scattered waves from the interaction zone, inasmuch as in the real experiments the decelerating system (and consequently also the region of localization of the lower-hybrid waves) have a finite dimension along the z axis. It is clear that such a mechanism of stabilization of the nonlinear processes will operate only if the wave energy is lost on account of linear (or quasilinear) dissipation mechanisms during one passage of the wave through the plasma. In the opposite case, the energy of the oscillations has time to become uniformly distributed over the entire plasma volume and there will be no convective stabilization mechanism. Numerical estimates show that in the existing tokamak installations (with characteristic parameters $\bar{n}_e \sim 10^{13} \text{ cm}^{-3}$, $T_e = 1 \text{ keV}$, $a \sim 10 \text{ m}$, $R \sim 50 \text{ cm}$) for oscillations with $\omega / |k_z| \gg V_{Te}$ (and most waves in the spectrum are of this kind)

and $\omega > \omega_{\text{LH}}^{\text{max}}$ all the linear dissipation mechanisms (Landau damping, dissipation due to the electron-ion collisions and to wave reflection from the chamber walls) are negligibly small, so that the noticeable energy absorption should take place after several hundred revolutions of the wave in the torus. Since experiments reveal never the less the absence of nonlinear processes at $\omega > \omega_{\text{LH}}^{\text{max}}$, it remains to assume that the lower-hybrid waves, say on account of quasilinear effects, produce on the periphery of the plasma pinch a layer of hot strongly absorbing plasma with $T_{e \text{ eF}} \sim 100 \text{ keV}$. The present paper is devoted to a theoretical investigation of the possible appearance of such "trapping" layer.

The problem is solved in the following formulation. A uniform plasma with temperature T_e , density n_e , and $\omega_{pe} < \omega_{Be}$ occupies the half-space $x \geq 0$. A source of lower-hybrid waves of frequency $\omega > \omega_{\text{LH}}$ is located in the $x=0$ plane and delivers a power P through 1 cm^2 of surface. Assume that the decelerating system excites the wave spectrum of large width with respect to k_z , such that $P_{k_z} = (Pk_o/k_z^2)\theta(|k_z| - k_o)$ ($k_o \approx 2\omega/c$ is the optimal deceleration). This form of the spectrum is close enough to that obtained in modern experiments. If the conditions $\omega/|k_z| > V_{Te}$ and $\omega < \omega_{pe}$ are satisfied, the oscillations propagate into the interior of the plasma with a group velocity $u_x = \omega^2/\omega_{pe}|k_z|$. In the absence of damping it is easy to obtain the spectral density of the energy of the waves in the plasma

$$W_{k_z} = \frac{|E|^2 k_z}{4\pi} = \frac{Pk_o}{\omega_{pe}|k_z|} \theta(|k_z| - k_o).$$

The fact that the decelerating system excites a wave spectrum that is broad with respect to k_z makes it possible to use the quasilinear theory to describe the reaction of the waves on the resonant electrons. In our case this equation can be written in the simplified form:

$$\frac{\partial f_z}{\partial t} = \frac{\partial}{\partial V_z} \int_{-\infty}^{\infty} dk_z Dk_z \delta\left(k_z - \frac{\omega}{V_z}\right) \frac{\partial f_z}{\partial V_z} - \nu_E (f_z - f_M). \quad (1)$$

Here

$$Dk_z = \frac{4\pi^2 e^2}{m^2} W_{k_z} \frac{k_z^2}{k^2} = \frac{4\pi^2 e^2 Pk_o}{m^2 \omega \omega_{pe}}; \quad f_z = 2\pi \int_0^{\infty} V_{\perp} dV_{\perp} f_e; \quad f_M = \frac{n_e}{\sqrt{\pi} V_{Te}} \exp\left(-\frac{V_z^2}{V_{Te}^2}\right); \quad \frac{1}{\nu_E}$$

$1/\nu_E$ is the energy lifetime of the electrons. The quantity ν_E is obtained from experiment and can greatly exceed the classical electronic thermal conductivity ($\nu_E \gg \chi_{e \text{ cl}}/a^2$). The stationary solution of (1) takes the form:

$$f_z \approx \frac{n_e}{2V_b} \exp\left(-\frac{|V_z|}{V_b}\right); \quad V_b = \sqrt{Dk_z/\nu_E}. \quad (2)$$

To estimate the value of V_b and to compare it with V_{Te} it is necessary to specify the numerical values of P , ν_E , n_e , T_e , etc. By way of example we have chosen the parameters of the TM- installation in typical discharges with lower-hybrid heating, the values of n_e , T_e , and ν_e being chosen from the conditions on the pinch periphery: $P=100 \text{ kW}$, $R=40 \text{ cm}$, $a=8 \text{ cm}$, $T_e=100 \text{ eV}$, $n_e=10^{12} \text{ cm}^{-3}$, and $\nu_E=10^8 \text{ sec}^{-1}$. For these parameters it turns out that $V_b \gtrsim 10^{10} \text{ cm/sec}$. We remark immediately that the "hot" plasma layer thickness (obtained from the energy-balance equation) is less than 1 cm in this case.

At $t < 1/\nu_E$, the distribution function varies with time like $f_z \sim \exp(-|V_z|/\sqrt{Dk_z t})$; the characteristic time necessary to establish the stationary state is $\tau \sim 1/\nu_E$.

We have thus shown that the quasilinear effects lead to the appearance of a thin layer of hot electrons, on the plasma periphery. If we estimate the decrement of the damping of the lower-hybrid waves by the resonant electrons in such a plasma, then we find that for waves with $|k_z| \lesssim (3/2)V_b \approx c/2$ we have:

$$\frac{\gamma}{\omega} \approx \frac{\omega \frac{\omega_{pe}^2}{k^2 n_e} \frac{\partial f_z}{\partial V_z} \Big|_{\omega/k_z}}{\omega} \approx \frac{\omega^2}{k_z^2 V_b^2} e^{-\frac{\omega}{|k_z| V_b}} \leq 1, \quad (3)$$

i.e., the wave must lose its energy over a length on the order of the transverse wavelength:

$$\Delta x \sim \frac{1}{k_x} \sim \frac{\lambda_z}{2\pi} \frac{\omega}{\omega_{pe}}. \quad (4)$$

It is interesting to note also that, in addition to the appearance of strong damping, for waves with $|k_z| < V_b$ ($N_z = |k_z|c/\omega \gtrsim 3$) the plasma becomes altogether opaque. Indeed, when the conditions $\omega < \omega_{pe}$ and $N_z > 1$ are satisfied, the expression for the transverse refractive index is⁽⁴⁾

$$N_{\perp}^2 \approx - (N_z^2 - 1) \left(1 - \frac{4\pi e^2 \infty}{m\omega} \int_{-\infty}^{\infty} \frac{V_z \frac{\partial f_z}{\partial V_z}}{\omega - k_z V_z} dV_z \right). \quad (5)$$

When the inequality $\omega/|k_z| < V_b$ is satisfied, it follows from (3) that

$$N_{\perp}^2 \approx - \frac{\omega_{pe}^2}{\omega^2} \frac{c^2}{V_b^2} \left(1 + i\sqrt{\pi} \exp\left(-\frac{\omega}{|k_z| V_b}\right) \right). \quad (6)$$

The appearance of such an opacity zone leads to an even greater localization of the waves on the plasma periphery. Thus, we have shown in this paper that the lower-hybrid waves can produce, on the periphery of a plasma pinch, on account of quasilinear effects, a hot plasma thin layer, thus leading to a strong kinetic absorption of the waves on the plasma periphery. It should be noted that the effectiveness of such a dissipation process depends substantially on the number of short-wave modes in the spectrum. Namely, the electron-acceleration mechanism begins to exceed the dynamical friction force only if the oscillation energy has a sufficiently large spectral density. If the number of short-wave modes in the excited spectrum is small, then the effective acceleration will be experienced only by the epithermal electrons with $V_z > V_0 > V_{Te}$, and consequently the number of accelerated particles (and correspondingly the wave damping decrement) will be exponentially small $\gamma/\omega \sim \exp(-V_0^2/V_{Te}^2)$. We note also that under certain conditions such a layer of hot plasma (relative to V_z) can be unstable to buildup of oscillations via the anomalous Doppler effect.

V.V. Alikhaev, Yu.I. Arsen'ev, G.A. Bobrovskii *et al.*, Zh. Tekh. Fiz. **45**, 523 (1975) [Sov. Phys. Tech. Phys. **20**, 327 (1975)]; W.M. Hook, Bull. Am. Phys. Soc. **20**, 1313 (1975); V.E. Golant *et al.*, Fifth Intern. Conf., Tokyo, 1973, IAEA-CN-33/A9-3; Tonon *et al.*, Third Intern. Congress on Waves and Instabilities in Plasma, Paris, 1977, A9-2.
M. Porkolab, Phys. Fluids **17**, 1432 (1974); C.S. Liu, Adv. Plasma Phys. **6**, 124 (1976); A.M. Rubenchik, Pis'ma Zh. Tekh. Fiz. **2**, 521 (1976) [Sov. Tech. Phys. Lett. **2**, 204 (1976)]; V.V. Parail, Preprint IAE-2608 1976.

³M. Porkolab, in: *Symposium on Plasma Heating in Toroidal Devices*, Varenna, 1974, Editrice Compositori, Bologna, 1974, p. 41; R.L. Berger, L. Chen, P.K. Kaw, and F.W. Perkins, *PPPI* 1308, 1976.

⁴T. Stix, *Theory of Plasma Waves*, McGraw, 1962.