

Development of instability and bubblon production on a charged surface of liquid helium

A. P. Volodin, M. S. Khaïkin, and V. S. Édel'man

Institute of Physics Problems, USSR Academy of Sciences

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The onset and development of an instability on a liquid-helium surface charged by electrons localized over the surface are investigated. It is established that the electrons leave the surface by formation of bubblons (bubbles filled with electrons) containing 10^7 – 10^8 electrons and having dimensions 0.05–0.03 mm. Small-diameter bubblons are stable in a field of 1 cgs esu and move in the helium with a steady-state velocity $\sim 10^4$ cm/sec.

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A liquid-helium surface can be negatively electrically charged by electrons localized over the surface.^[1] An equilibrium charged helium surface is produced in an electric field under the influence of gravitational, capillary, and electrostatic forces. There exist, however, critical values of the electric field (or of the charge density) above which a flat surface becomes unstable. Gor'kic and Chernikova have determined the conditions under which a charged helium surface becomes unstable.^[2,3] Owing to the instability, the attained surface-charge density has an upper bound $\sim 2 \times 10^9$ electrons/cm², a value previously observed in experiment.^[4,5]

In our article we describe experiments aimed at investigating the conditions for the appearance of the instability, as well as the mechanism whereby the electrons leave the helium surface. The experiments were performed at $T \sim 1.3$ K in the assembly schematically shown in Fig. 1. The electron source was an incandescent tungsten filament 1. The voltage that produced the field which retained the electrons on the helium surface 2 was applied to the electrodes of the capacitor. The lower, positively charged, plate 3 was surrounded by a screening ring 4. The upper grounded plate 5 was suspended on springs and could move in a vertical direction in the gap between it and the charged helium surface. The plate position was measured with a capacitive pickup 6 and served as a measure of the field E_z . The level of the superfluid helium in the capacitor was regulated via the

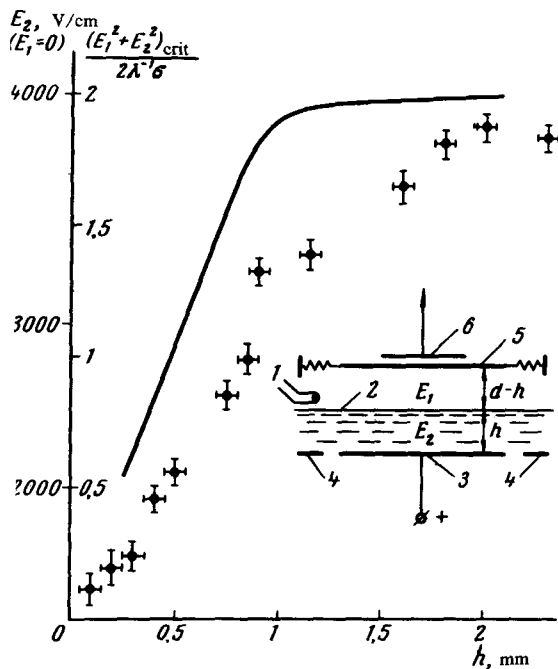


FIG. 1. Dependence of the critical parameter $(E_1^2 + E_2^2)_{\text{crit}}$ at which a flat uniform surface of liquid helium becomes unstable, on the depth h of the helium in the capacitor. Points—experiment, curves—calculation.^[3]

hermomechanical effect.^[6] The capacitor plates, of 40 mm diameter, were positioned parallel to the helium surface with accuracy $30''$ as determined by the maximum of the critical parameter (see below). The distance d between the plates was set in the range 1–5 mm. The assembly was placed in an optical cryostat fastened onto a platform suspended on soft shock absorbers. To investigate the dynamics of the phenomenon, we used high-speed (up to 4000 frames/sec) photography with an SKS-1M-16 camera.

At a certain initial position of the helium level h_0 and a voltage U_0 applied to the capacitor, electrons were emitted from cathode 1, which was turned on for a time ~ 0.1 sec. The appearance of the surface charge manifested itself in a complete screening of the field over the helium surface, i.e., $E_1 = 0$. The critical conditions for the charged helium surface were then attained either by slowly lowering the helium level h in the instrument, or by increasing the voltage U . The field E_1 was recorded as a function of the varied parameter.

High-speed photographs were simultaneously taken of the surface and volume of the liquid helium.

The experiments have shown that when the critical conditions, determined in the general case by the parameters U_0, h_0, h , or U_0, h_0, U were reached, capillary-gravitational waves with amplitude ~ 0.5 mm were excited on the helium surface after times 0.03–0.1 sec and the surface charge vanished after 0.1–0.3 sec. This is evidence of a "hard" regime of instability development.^[7]

The measured dependence of the critical quantity $(E_1^2 + E_2^2)_{\text{crit}}$ on the helium level height h is shown in Fig. 1. In the figure are gathered points obtained at an experimental geometry close to that at which the quantity $(E_1^2 + E_2^2)$ is a single-valued critical parameter, i.e., at $h = d/2$ or $d < h$.^[3] The experimental dependence (points) is in satisfactory agreement with the calculation of Chernikova^[3] (curve).

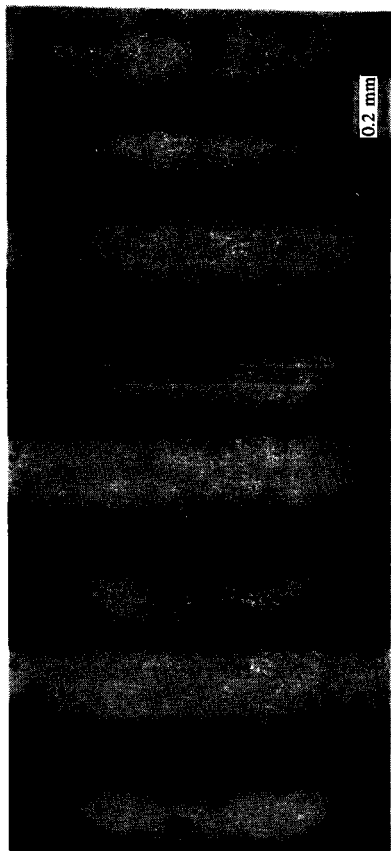


FIG. 2. Motion-picture frames showing the onset of capillary waves and of bubblons that carry away electrons from the charged helium surface when the latter becomes unstable.

The change in the character of the dependence at $h \approx 1-1.5$ mm corresponds to a transition from instability with respect to long-wave perturbations to instability with characteristic oscillation wavelengths of the order of the capillary wavelength $\lambda = 3.2$ mm. This is confirmed by an analysis of the photograph frames: at $h \leq 0.6-0.7$ mm waves of length 2-3 cm, i.e., on the order of the dimensions of the capacitor plates, are excited on the helium surface, whereas at $h \gtrsim 1.5$ mm the excited waves are 2-5 mm long.

Motion picture photography has made it possible to trace the departure of the electrons from the helium surface. Figure 2 shows four frames of the film. The first on the top shows a uniform stable surface. The flat uniformly charged helium surface is lowered by the electrostatic forces of the capacitor to 0.2 mm below the helium level in the cryostat; both levels are shown on the frame. When instability sets in and surface waves build up, sharp dips are observed in valleys (Fig. 2, second frame). At the tips of the dips are produced bubbles (frame 3) with dimensions from 0.05 to 0.3 mm; these bubbles then penetrate into the helium (fourth frame). After reaching the bottom—the anode of the capacitor—the bubble either vanishes or floats upwards, depending on its size: bubbles with 0.5 mm diameter collapse at the bottom within a time $\tau \leq 10^{-4}$ sec, while the larger have a lifetime 10^{-3} sec long enough to float upwards.

The cause of the observed phenomenon is that each bubble constitutes a multiply charged (10^7-10^8 electrons) negative ion—bubblon—in the superfluid helium. The bubblon moves toward

the anode, where it is discharged upon contact; the remaining bubble with the gas collapses. From the condition that the electrostatic pressure from inside the bubble be equal to the capillary pressure we obtain for the bubble radius an estimate $r \sim \sqrt[3]{n^2 e^2 / 16 \pi \sigma} \sim 8 \times 10^{-3}$ cm, where e is the electron charge, σ is the surface tension of the liquid helium, and n is the number of electrons in the bubble and is determined from the total charge of the surface and the number of bubbles that discharge the surface (20–100).

It appears that the entire charge is carried away from the helium surface by the bubbles, inasmuch as such a process is energywise more favored than the departure of individual electrons into the liquid helium. The electrons could in principle depart via the tunnel effect, but theoretical estimates show that the probability of this effect is negligibly small,^[1] and in experiment at $E_1^2 + E_2^2 < (E_1^2 + E_2^2)_{\text{crit}}$ the electrons remain over the helium surface for hours.

Bubbles with small diameter, 0.05 mm, move in the liquid helium in a field $E = 1$ cgs esu with velocity 10^4 cm/sec, which corresponds to Stokes viscous motion. The time to move to the bottom is $\sim 10^{-3}$ sec, which is much longer than the relaxation times of the electric and other inhomogeneities over their dimensions. At the same time, the lower modes of the natural oscillations of the bubbles should have wavelengths of the order of the bubble dimensions, i.e., smaller by a factor of 10^2 than the capillary wavelength λ , thus ensuring a relative stability of the bubble. Small-diameter bubbles should therefore be regarded as stationary formations.

As the result of electrostatic interaction, the electrons in the bubble form a two-dimensional layer near the surface of the liquid. The electron density is 10^{11} – 10^{12} cm⁻²—so high, that the layer can be regarded as flat and its Wigner crystallization seems quite probable.^[1] It must be emphasized in conclusion that bubbles are an interesting subject of study as perfectly new physical objects.

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