

# Effect of a magnetic field on the longitudinal spin relaxation of $\mu^+$ in isotropic ferromagnets in the critical paramagnetic vicinity of $T_C$

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A theory is derived for the behavior of the longitudinal spin relaxation  $\Lambda_{\parallel}(\tau, H)$  of muons as a function of the magnetic field  $H$  in ferromagnets in the critical region above  $T_C$ . The results show that a study of  $\Lambda_{\parallel}(\tau, H)$  would make it possible to determine the spin diffusion coefficient of the magnetic material.

The  $\mu SR$  method has been used to study the critical behavior of the ferromagnetic metals Ni and Pd (2.0 at.% Mn).<sup>1,2</sup> In the paramagnetic phase, the spin relaxation rate of  $\mu^+$  has been observed to increase toward  $T_C$  because of a critical retardation of spin fluctuations of the magnetic metal atoms. It also turns out that applying a relatively weak magnetic field  $H$  causes a qualitative change in the temperature dependence of  $\Lambda_{\parallel}(\tau, H)$  [ $\tau = (T - T_C)/T_C$ ] (Ref. 2). No systematic study has been made of the  $H$  dependence of  $\Lambda_{\parallel}(\tau, H)$ , and the effect observed in Ref. 2 has not been theoretically explained.

Let us examine the effect of  $H$  on  $\Lambda_{\parallel}$  in cubic ferromagnets near  $T_C$ . We will show that a study of  $\Lambda_{\parallel}(\tau, H)$  would offer a unique opportunity for studying the hydrodynamic region of critical fluctuations in ferromagnetic metals. In particular,

such a study would make it possible to work from the  $\mu SR$  data to determine the spin diffusion coefficient  $D$ . The question of a determination of  $D$  by an ESR method was studied in Ref. 3. On the basis of that analysis, values were found for  $D$  for the ferromagnetic semiconductors  $CdCr_2Se_4$  and  $CdCr_2S_4$  (Ref. 4). However, the ESR techniques are severely limited in metals, and we know of no experimental study on ESR in metals in the critical region above  $T_C$ .

We write the interaction of the magnetic moment  $\frac{1}{2}\gamma_\mu \vec{\sigma}$  of a muon localized at the position  $\mathbf{r}_\mu$ , with magnetic moments  $g\mu S$  of the magnetic material at sites  $\mathbf{l}$ , as follows:

$$V(\mathbf{r}_\mu) = \frac{1}{2} \gamma_\mu g\mu \sum_{\mathbf{l}} \sum_{\alpha, \beta} \sigma_\alpha(\mathbf{r}_\mu) \widehat{\mathcal{F}}_{\alpha\beta}(\mathbf{r}_\mu - \mathbf{l}) S_\beta(\mathbf{l}) \quad (1)$$

Here  $\widehat{\mathcal{F}}$  is a tensor which in metals is determined by dipole forces and by an isotropic hyperfine interaction with a constant  $A_{hf}$ . For  $\widehat{\mathcal{F}}$  in the  $\mathbf{q}$  representation, which we will need below, we have the expression

$$\widehat{\mathcal{F}}_{\alpha\beta}(\mathbf{q}) = \frac{4\pi}{v_0} \frac{1}{3} \delta_{\alpha\beta} - \frac{q_\alpha q_\beta}{q^2} + \frac{1}{v_0} A_{hf} \delta_{\alpha\beta} \quad (2)$$

where  $v_0$  is the volume of the unit magnetic cell. Introducing a retarded binary spin Green's function  $\widehat{G}(\mathbf{q}, \omega)$  of the magnetic material, and using (1) and (2), we find the following expression for  $\Lambda_{\parallel}$  in a coordinate system with  $z$  axis running along  $\mathbf{H}$ :

$$\Lambda_{\parallel}(\tau, H) = (\gamma_\mu g\mu)^2 \sum_{\alpha=x, y} \sum_{\beta, \rho} \frac{v_0}{(2\pi)^3} \int d\mathbf{q} \widehat{\mathcal{F}}_{\alpha\beta}(\mathbf{q}) \widehat{\mathcal{F}}_{\alpha\rho}(\mathbf{q}) \frac{T_C \text{Im} G_{\beta\rho}(\mathbf{q}, \omega, \mathbf{H})}{\omega} \Big|_{\omega = \omega_\mu} \quad (3)$$

where  $\omega_\mu$  is the precession frequency of the  $\mu^+$ . In deriving (3) we allowed for the fact that in cubic ferromagnetic metals  $\mu^+$  localizes in either octahedral or tetrahedral voids. Expression (3) is essentially the well-known perturbation-theory result used in NMR.<sup>5,6</sup>

Let us examine the exchange temperature region, in which the magnetic susceptibility satisfies  $4\pi\chi(\tau) \ll 1$ ; we begin with the case of a weak field,<sup>8</sup>  $g\mu H \ll T_C \tau^{5/3}$ . In a zero field, using the hypothesis of dynamic similarity for  $G$ , we easily find<sup>6</sup>  $\Lambda_{\parallel}(\tau, 0) \equiv \Lambda(\tau) \propto \tau^{-1}$ . As was shown in Ref. 3, in a weak field there is a substantial change in only the dynamics of transverse spin hydrodynamic fluctuations. The corresponding expression for the cyclic components  $C_{\pm\mp}$  under the condition  $q \ll R_C^{-1}$  ( $R_C \propto \tau^{-2/3}$  is the correlation radius) is

$$G_{+-}(q, \omega, H) = G_{-+}(q, \omega, -H) = G_0(\tau) \frac{-g\mu H + iD(\tau)q^2}{\omega - g\mu H + iD(\tau)q^2} \quad (4)$$

where  $G_0$  is the static Green's function. As a result, the transverse components of  $\widehat{G}$  determine the field dependence of  $\Lambda_{\parallel}$ , for which we find from (1)–(4), ignoring  $\omega_\mu$  in comparison with  $g\mu H$ ,

$$\Delta\Lambda_{\parallel}(\tau, H) = \Lambda_{\parallel}(\tau, H) - \Lambda(\tau) = -c_1 \frac{(\gamma_{\mu} g\mu)^2}{v_0} T_C G_0(\tau) \frac{(g\mu H)^{1/2}}{D(\tau)^{3/2}}, \quad (5)$$

$$c_1 = \frac{\pi}{\sqrt{2}} \frac{56}{45} + \frac{2}{(2\pi)^2} A_{hf}^2.$$

We see that applying a field  $H$  reduces  $\Lambda$ . The proportionality  $\Delta\Lambda_{\parallel} \propto H^{1/2} D^{-3/2}$  is a direct consequence of the circumstance that a fluctuating field acting on the  $\mu^+$  spin contains a nonlocal hydrodynamic diffusion mode. A study of  $\Delta\Lambda_{\parallel}(\tau, H)$  will make it possible to determine  $D$  if the  $A_{hf}$  are known and if we know  $\chi(\tau)$  from static measurements. The latter quantity is related to  $G_0(\tau)$  by  $4\pi\chi = \omega_0 G_0$  [ $\omega_0 = 4\pi(g\mu)^2 v_0^{-1}$ ]. For this purpose, at a fixed value of  $\tau$ , we need to find the interval of  $H$  in which the relation  $\Delta\Lambda_{\parallel} \propto H^{1/2}$  holds. As is clear from (5), the proportionality coefficient in this dependence determines  $D(\tau)$ .

We ignored the uniform dipole damping of  $\Gamma_d$  above.<sup>9</sup> When we take it into account,  $Dq^2$  in (4) acquires an increment<sup>3</sup>  $\Gamma_d$ , which in turn leads to a replacement of  $(g\mu H)^{1/2}$  in (5) by  $\{[(g\mu H)^2 + \Gamma_d^2]^{1/2} + \Gamma_d\}^{1/2} - (2\Gamma_d)^{1/2}$ . Expression (5) thus holds at  $T_C \tau^{5/3} \gg g\mu H \gg \Gamma_d$ .

Let us examine  $\Lambda_{\parallel}(\tau, H)$  in the case of a field which is not too weak ( $g\mu H \gg \Gamma_d$ ) but which is otherwise arbitrary. Working from the hypothesis of dynamic similarity in a field,<sup>6</sup> we find

$$\Lambda_{\parallel}(\tau, H) = \frac{\Lambda_0}{\tau} \varphi\left(\frac{h}{\tau^{5/3}}\right), \quad h = \frac{g\mu H}{T_C}, \quad (6)$$

where  $\varphi(0) = 1$ , and  $\Lambda_0 \sim (\gamma_{\mu} g\mu/v_0)^2 T_C^{-1}$ . In (5) we have actually determined the first term in an expansion of  $\varphi(x)$  under the condition  $x \ll 1$ . Since  $D \propto \tau^{1/3}$  and  $G_0(\tau) \propto \tau^{-4/3}$  (Ref. 6), we find from (5)  $\varphi(x) = 1 - c\sqrt{x}$ , where  $c \sim 1$ . We must emphasize that a weak field has a greater effect on  $\Lambda_{\parallel}$  than on the static quantities, to which the corrections are on the order of  $(h/\tau^{5/3})^2$ . In a strong field ( $h \gg \tau^{5/3}$ ),  $\Lambda_{\parallel}$  depends primarily on  $H$ . As follows from (6), we have  $\Lambda_{\parallel}(0, H) \propto H^{-3/5}$ . It is not possible to theoretically determine whether  $\Lambda_{\parallel}$  remains a monotonic function of  $\tau$  or goes through a maximum when a field  $H$  is applied. A maximum was observed in Ref. 2. By virtue of (6), its position would then be  $\tau_m \propto H^{3/5}$ , and we would have  $\Lambda_{\parallel}(\tau_m, H) \propto H^{-3/5}$ .

Let us take a closer look at Ref. 2, where a study was made of  $\Lambda_{\parallel}$  in PdMn above  $T_C$ . At  $H = 0$ , the rate  $\Lambda$  increased with decreasing  $T$ , all the way to  $T_C = 5.8$  K. In a field  $H = 5$  kOe, a maximum appeared in the dependence  $\Lambda_{\parallel}(\tau)$  at  $T_m = 10$  K ( $\tau_m \approx 0.7$ ). Using  $g_{\text{eff}} = 2.7$  for Mn in Pd (Ref. 2), we find that at  $\tau = \tau_m$  the corrections to the static quantities are  $(h/\tau_m^{5/3})^2 \approx 7 \times 10^{-2}$ , whereas  $\Lambda$  decreases more than twofold:  $\Lambda_{\parallel}(\tau_m, H) \approx 0.4\Lambda(\tau_m)$ . Such a sharp change in  $\Lambda$  in a statically weak field is evidence that a field dependence of  $\Lambda_{\parallel}$  of a "diffusion" nature was probably observed in Ref. 2.

Finally, since we have  $\Lambda_{||}(0, h) = c_1 \Lambda_0 h^{-3/5}$  by virtue of (6), we find from the experimental results that the constant  $c_1$  satisfies  $c_1 \ll 1$ .

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