

# Interaction of charge carriers in multiparticle exciton-impurity complexes in silicon

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It is shown that the “natural” width of bound-exciton emission lines in phosphorus-doped silicon does not exceed  $5 \mu\text{eV}$  and that the emission lines of multiparticle complexes have a large number of components whose splitting is explained by the interaction between the holes and between the holes and the outer electrons.

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We have used the interference method<sup>1</sup> to investigate the shape and fine structure of the phononless emission lines  $\alpha_m$  of the multiparticle exciton-impurity complexes  $P_m$  bound by phosphorus atoms in silicon ( $m$  is the number of electron-hole pairs). The fine structure appears as a result of interaction of charge carriers in the complexes, which splits the initial  $P_m$  state and the final  $P_{m-1}$  state.<sup>2,3</sup> The  $\alpha_1$  line does not have a

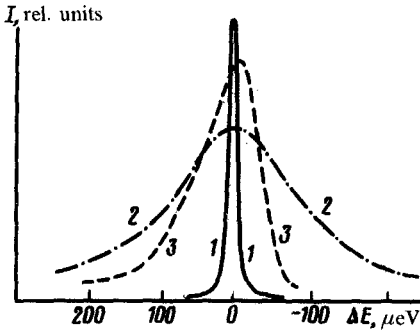


FIG. 1. Phononless emission lines of excitons bound to phosphorus atoms (concentration  $P_0 = 2 \times 10^{14} \text{ cm}^{-3}$ ) in silicon at 4.2 K. Neutron-doped sample SV - 1: 1,  $\alpha_1$  line; 2,  $\alpha_1^{2S}$  line. Sample with phosphorus concentration of  $7 \times 10^{17} \text{ cm}^{-3}$  grown in a quartz crucible: 3,  $\alpha_1$  line.

fine structure, since the two electrons, which form the singlet  $\Gamma_1(ee)$ , cannot split the hole level  $\Gamma_8$  in the initial state  $P_1\{\Gamma_8(h)\Gamma_1(ee)\}$ , while the final state  $P_0\{\Gamma_1(e)\}$  has only one electron. Therefore, an analysis of the shape of the  $\alpha_1$  line makes it possible to draw conclusions about the broadening and splitting of the emission lines of complexes, which are not related to charge-carrier interaction. We can see in Fig. 1 that the narrowest  $\alpha_1$  line is observed in silicon crystals grown by the crucibleless zone crystallization method and doped with phosphorus by means of neutron irradiation. The width of the  $\alpha_1$  line, with allowance for the finite resolution, does not exceed  $5 \mu\text{eV}$ . In the decay of  $P_1$  with the production of a donor in the excited  $2S$  state the  $\alpha_1^{2S}$  line is broadened considerably compared with  $\alpha_1$ , because of the small lifetime  $\sim 5 \times 10^{12} \text{ sec}$  of the excited state. A strong inhomogeneous broadening of the  $\alpha_1$  line was observed in crystals grown from quartz crucibles and therefore containing an appreciable ( $\sim 10^{18} \text{ cm}^{-3}$ ) concentration of oxygen. The imperfect crystals investigated in Ref. 3 apparently caused a broadening of the  $\alpha_1$  line to  $50 \mu\text{eV}$ , an unsatisfactory resolution of the structure of the  $\alpha_2$  line and an erroneous interpretation of the results.

It can be seen in Fig. 2 that the  $\alpha_2$  emission line consists of a large number of components whose splitting is due to the interaction of charge carriers in the initial state  $P_2\{\Gamma_8(hh)\Gamma_1(ee)\Gamma_{35}(e)\}$  and the final state  $P_1\{\Gamma_8(h)\Gamma_1(e)\Gamma_{35}(e)\}$ . The main feature of this splitting can be explained by taking into account only the interaction between the holes and the exchange interaction of holes with an electron of the outer  $\Gamma_5$  shell. Interaction with electrons in the  $\Gamma_1$  shell can be ignored, since this shell in  $P_2$  is filled, and the electron in  $P_1$ , which remains in a highly localized orbital, does not interact strongly with the rest of the charge carriers. The  $\Gamma_3$  electron shell at 2K must be slightly populated, since it lies in  $P_1$  above the  $\Gamma_5$  shell by approximately<sup>4</sup>  $600 \mu\text{eV}$ . Since the anisotropy of the effective electron mass in silicon is not very large and since the crystal splitting  $\Gamma_8(h) \times \Gamma_5(e)$  must be slight, we shall assume that the wave function of the electron in the  $\Gamma_5$  shell is transformed as a  $\Gamma_6$  spinor. In these approximations the initial state in the  $P_2$  complex must split into four levels  $\{\Gamma_8(h) \times \Gamma_8(h)\} \times \Gamma_6(e) = \Gamma_6 + \Gamma_7 + \Gamma_8 + \Gamma_8$ . The final  $P_1$  state is split into three levels  $\Gamma_8(h) \times \Gamma_6(e) = \Gamma_3 + \Gamma_4 + \Gamma_5$ . The splitting scheme for the structure of the  $\alpha_2$  line is shown in Fig. 2. To compare the experimental spectrum with the diagram, we have

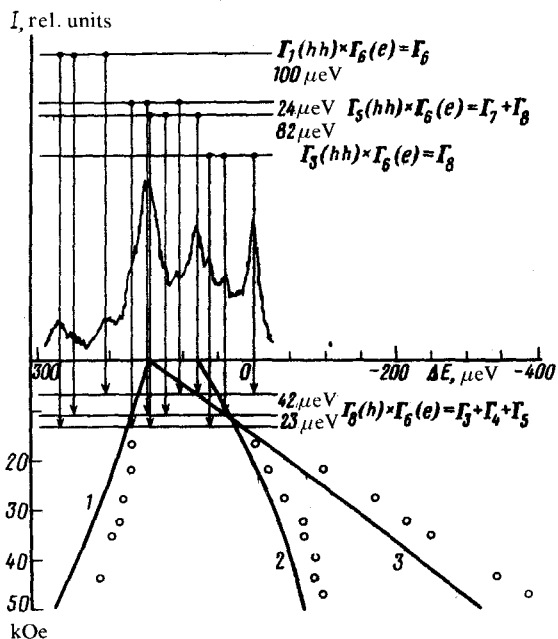


FIG. 2. Fine structure of the  $\alpha_2$  line of sample SV - 1 at 2K and  $H = 0$ . The arrows depicting the transitions from the initial  $P_2$  state to the final  $P_1$  state indicate the predicted location of the emission lines along the horizontal energy axis, in accordance with the splitting of the  $P_2$  and  $P_1$  levels in the diagram. The Zeeman components of the  $\alpha_2$  line (circles) are plotted in the lower part of the figure as a function of the intensity of the magnetic field  $\mathbf{H} \parallel (111)$ . The dependence of the shift of the Zeeman components of the  $\alpha_1$  line on  $H$  (solid curves) for the analogous electron transitions is also shown there.

matched the arrow corresponding to the radiative transition with minimum energy on the horizontal energy scale with the location of the longest wavelength component of the spectrum and the location of the remaining arrows illustrating the transitions is determined by the splitting of the initial and final states indicated in the diagram. We can see in Fig. 2 that this scheme describes well the structure of the  $\alpha_2$  line

The Zeeman spectrum of  $\alpha_2$  in a magnetic field  $H \gg 20$  kOe consists of three main components<sup>5</sup>

$$P_2 \left\{ \Gamma_8 \left( -\frac{3}{2}, -\frac{1}{2} \right) \Gamma_1 \left( +\frac{1}{2}, -\frac{1}{2} \right) \Gamma_5 \left( -\frac{1}{2} \right) \right\} \rightarrow P_1 \begin{cases} \left\{ \Gamma_8 \left( -\frac{3}{2} \right) \Gamma_1 \left( -\frac{1}{2} \right) \Gamma_5 \left( -\frac{1}{2} \right) \right\} & (1) \\ \left\{ \Gamma_8 \left( -\frac{1}{2} \right) \Gamma_1 \left( -\frac{1}{2} \right) \Gamma_5 \left( -\frac{1}{2} \right) \right\} & (2) \\ \left\{ \Gamma_8 \left( -\frac{3}{2} \right) \Gamma_1 \left( +\frac{1}{2} \right) \Gamma_5 \left( -\frac{1}{2} \right) \right\} & (3) \end{cases}$$

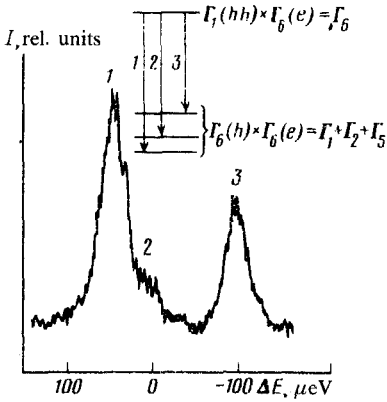


FIG. 3. Fine structure of the  $\alpha_2$  line at 2K produced as a result of compression ( $390 \text{ kgf/cm}^2$ ) of the SV — 1 sample in the (001) direction.

whose location is plotted in Fig. 2 as a function of  $H$ . The dependence on  $H$  of the shift of the Zeeman components of the  $\alpha_1$  line for the corresponding electron transitions is represented by the solid lines in Fig. 2. We can see in Fig. 2 that the dependence of the shift of the Zeeman components of the  $\alpha_2$  line is close to that for the analogous components of the  $\alpha_1$  line. Used in the identification of the transitions, this fact made it possible to reliably identify the spectral regions of the  $\alpha_2$  line from which the corresponding Zeeman components originate. We can see that the components 1 and 3 of the  $\alpha_2$  line originate from the same spectral region at  $H=0$ , and the component 2 arises from another region of the original spectrum. It follows from this that the interaction between a hole and an electron of the outer  $\Gamma_5$  shell gives the major contribution to the splitting of the final state  $P_1$ , while the interaction with the electron of the  $\Gamma_1$  shell does not result in noticeable splitting.

When the silicon is compressed in the (001) direction, the symmetry is reduced to  $D_{2d}$  and the lowest energy state of the holes is  $\Gamma_6$  with the moment  $\frac{1}{2}$ , which is degenerated only in spin. The electron state  $\Gamma_1$  is not split, while the  $\Gamma_{35}$  state is split into several branches, the lowest of which corresponds to the nondegenerate  $\Gamma_4$  state. Thus, the ground state  $P_2$  is not split with uniaxial compression. The final state  $P_1$  is split into three states  $\Gamma_6(h) \times \Gamma_6(e) = \Gamma_1 + \Gamma_2 + \Gamma_3$ , because of the exchange interaction of a hole with an electron from the outer  $\Gamma_4$  shell. The spectrum of the  $\alpha_2$  line for uniaxial compression along (001) is shown in Fig. 3, together with the transition scheme. We note that the  $\alpha_2$  line is also a triplet as a result of stretching along the (001) axis; this confirms the validity of these approximations.

Thus, the proposed model makes it possible to explain the fine structure of the  $\alpha_2$  line and its splitting in magnetic and strain fields.

The asymmetric spectra of the  $\alpha_3$  and  $\alpha_4$  lines have a large number of anomalies, which indicates that they consist of many components. However, the individual components could not be resolved, probably because of their noticeable broadening, since the  $P_{m-1}$  complexes are produced in the excited state as a result of emission of the

$\alpha_m$  line. In this case the time of relaxation of one of the  $m - 1$  electrons of the  $\Gamma_{35}$  shell to a partially filled  $\Gamma_1$  shell must decrease as  $m$  increases.

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