

from formulas (4). In calculating $\langle \pi^- | S_+ | n \rangle$ we took the n - X mixing into account (for details see [5]). The empirical values of S_1 in Table II were taken from [2], with due allowance for f - f' mixing with an angle $\theta = 30^\circ$, i.e., the same as for the f and f' mesons [6]. In addition, the constants S_1 turned out to be sensitive to the choice of v_8^S/v_3^S in formula (3), and therefore this ratio was chosen to agree with experiment; $v_8^S \sim v_3^S$ in order of magnitude, as required by SU(3) symmetry.

We emphasize that the constants S_1 used by us were obtained in [2] by reduction of experimental data under the assumption that the cross sections are constant, $\alpha_f = 1$. Therefore the fact that theory and experiment agree in Table II within the $\sim 20\%$ accuracy of SU(3) symmetry means that there is no contradiction whatever between the hypothesis of universal interaction of the T reggeons (2) and the hypothesis of constant cross sections.

Thus, the hypothesis of the universal interaction of the reggeons with vector and scalar currents has so far been well justified.

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- [1] N. Cabibbo, L. Horwitz, and Y. Ne'eman, CERN Preprint TH.680, 1966.
- [2] K. A. Ter-Martirosyan, ITEP Preprint No. 494, 1967.
- [3] N. Cabibbo, L. Horwitz, J. Kokkedee, and Y. Ne'eman, CERN Preprint TH.685, 1966.
- [4] I. Yu. Kobzarev, in: Voprosy fiziki elementarnykh chastits (Problems of Elementary-particle Physics), v. 5, Erevan, 1966, p. 66.
- [5] A. A. Migdal, *ibid.* v. 6, 1967.
- [6] A. H. Rosenfeld et al. *Revs. Modern Phys.*, January, 1967.

CONTRIBUTION OF UNPAIRED PARTICLE TO THE DEFORMATION OF THE NUCLEUS

E. E. Berlovich and Yu. N. Novikov
 A. F. Ioffe Physico-technical Institute, USSR Academy of Sciences
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It was shown in [1] that the experimental values of the internal quadrupole moments θ_0 of certain odd deformed nuclei differ greatly from the values of θ_0 of the preceding even-even nuclei. These changes in the quadrupole moments, which are due to the presence of unpaired particles, reach about 10 - 20% in some cases. The contribution to the quadrupole moment is positive in some cases and negative in others.

It is possible to estimate the contribution of the odd particle to the deformation of the nucleus by calculating the equilibrium deformations of the odd and preceding even-even nuclei. We have minimized the sum of the doubly-degenerate single-particle energies corresponding to the Hamiltonian

$$H = T_{\text{kin}} + \frac{M}{2} \omega_0^2 (\epsilon) r^2 (1 + \epsilon P_2(\cos \theta)) - c |s| - D [l^2 - \langle l^2 \rangle_{\text{shell}}],$$

where ω_0 is the oscillator frequency, ϵ the deformation parameter, and C and D are parameters that are the same for all shells of like nucleons in the investigated nucleus. This Hamiltonian was proposed in [2] and represents ϵ modification of the universally known expression used in [3].

Just as in [4,5], we disregard the pairing forces and the Coulomb energy, which act in opposite directions. The pairing effect predominates at low deformations [6, 7] and the influence of the Coulomb energy becomes dominating at large deformations, especially in heavy nuclei [2,7]. However, the magnitudes of these effects will be subtracted in determining the difference of the equilibrium deformations $\Delta\epsilon_0 = \epsilon_0(A + 1) - \epsilon_0(A)$ of two nuclei with neighboring mass numbers A. In addition, the plot of the total energy $E(\epsilon)$ (including the Coulomb and pairing energies) against the deformation has a much broader minimum than the plot without allowance for the energies, and when the equilibrium deformation is determined with allowance for these two factors the error is larger [8]. It was therefore deemed expedient to estimate the difference $\Delta\epsilon_0$ by using the method of minimizing the single-nucleon energies.

The single-particle levels of the protons and neutrons at values $\epsilon = 0, 0.1, 0.2, 0.3, 0.4,$ and 0.5 were tabulated by V. V. Pashkevich. The parameter C was chosen equal to $-0.1274 \times \hbar\omega_0$ for both neutrons and protons, and the parameter D equal to $-0.03822\hbar\omega_0$ for protons and $-0.02675\hbar\omega_0$ for neutrons [2].

We used these data to calculate the equilibrium deformations of even-even and odd nuclei for which the experimental values of the quadrupole moments are known [1]. The differences $\Delta\epsilon_0$ of neighboring nuclei are listed in the table. The experimental values of the equilibrium

Comparison of experimental and theoretical values of $\Delta\epsilon_0$

$A+1 Z(\Omega\pi[Nn_z A]) - AZ'$	$\Delta\epsilon_0$ exp.	$\Delta\epsilon_0$ theor.
$^{153}\text{Eu}(p\ 5/2+[413]) - ^{152}\text{Sm}$	0.024 ₅	0.015 or 0.04
$^{155}\text{Gd}(n\ 3/2-[521]) - ^{154}\text{Gd}$	0.006 ₇	< 0.01
$^{157}\text{Gd}(n\ 3/2-[521]) - ^{156}\text{Gd}$	-0.008 ₇	< 0.01
$^{159}\text{Tb}(p\ 3/2+[411]) - ^{158}\text{Gd}$	0.005 ₅	< 0.01
$^{161}\text{Dy}(n\ 5/2+[642]) - ^{160}\text{Dy}$	0.021 ₁₀	0.01
$^{163}\text{Dy}(n\ 5/2-[523]) - ^{162}\text{Dy}$	0.002 ₈	< 0.01
$^{165}\text{Ho}(p\ 7/2-[523]) - ^{164}\text{Dy}$	-0.004 ₇	< 0.01
$^{167}\text{Er}(n\ 7/2+[633]) - ^{166}\text{Er}$	0.003 ₅	< 0.01
$^{173}\text{Yb}(n\ 5/2-[512]) - ^{172}\text{Yb}$	-0.004 ₇	< 0.01
$^{175}\text{Lu}(p\ 7/2+[404]) - ^{174}\text{Yb}$	-0.020 ₅	-0.02
$^{177}\text{Lu}(p\ 7/2+[404]) - ^{176}\text{Yb}$	-0.031 ₈	-0.02
$^{177}\text{Hf}(n\ 7/2-[514]) - ^{176}\text{Hf}$	-0.022 ₇	-0.02
$^{179}\text{Hf}(n\ 9/2+[624]) - ^{178}\text{Hf}$	-0.001 ₇	< 0.01
$^{181}\text{Ta}(p\ 7/2+[404]) - ^{180}\text{Hf}$	-0.021 ₆	-0.02
$^{187}\text{Re}(p\ 5/2+[402]) - ^{186}\text{W}$	-0.026 ₁₄	-0.02
$^{189}\text{Os}(n\ 3/2-[512]) - ^{188}\text{Os}$	-0.008 ₁₂	< 0.01
$^{191}\text{Ir}(p\ 3/2+[402]) - ^{190}\text{Os}$	-0.039 ₆	-0.04

deformations were determined from the relation

$$Q_0 = 0,8 ZR_0^2 \epsilon_0 (1 + 1/2 \epsilon_0)$$

using mean-weighted data on the internal quadrupole moments Q_0 [1]. Theoretical calculations of ϵ_0 were made for those level combinations under the Fermi surface, which corresponded to the experimental values of the spin, parity, and quadrupole moment of the nucleus.

Addition of an unpaired particle to an even-even core leads to a slight change in the order of the level occupation only in the case of the nuclei ^{153}Eu and ^{191}Ir . In the remaining

cases listed in the table, the sets of configurations entering in the total sum of the energies coincide in the even and odd nuclei (with the exception of the last unpaired particle). The change in the equilibrium deformation is therefore due entirely to the character of the polarization of the core by this particle.

If the particle fills a descending orbital of the single-particle scheme [2], then the minimum of the total energy shifts upon addition of this particle to the region of larger deformations; on the other hand, if it populates an ascending orbital, the shift is towards lower values of the deformation. Horizontal orbitals do not cause shifts of the minima. The magnitude of the shift is determined by the slope of the orbital of the unpaired nucleon. This is seen from the table, where steep orbitals in the nuclei ^{161}Dy , $^{175,177}\text{Lu}$, ^{177}Hf , ^{181}Ta , and ^{187}Re correspond to a larger shift of both the calculated and experimental values of ϵ_0 . In the nuclei ^{153}Eu and ^{191}Ir , a large change in the values of the deformations, compared with those of the preceding ^{152}Sm and ^{190}Os respectively, is obtained as the result of changes in one or two orbitals in the set of configurations. Such changes in the set of configurations under the Fermi surface are quite typical of nuclei in the transition regions or directly adjoining them [9]. Such nuclei include ^{153}Eu and ^{191}Ir [10]. In the remaining cases listed in the table, the shifts of the minima of the $E(\epsilon)$ curves upon addition of an unpaired nucleon lie within the limits of the accuracy with which the values of ϵ_0 are interpolated, and therefore only the upper limits are given for the differences $\Delta\epsilon_0$.

As seen from the table, there is good agreement between the experimental values and the theoretical estimates of the contribution of the unpaired nucleon to the deformation of the nucleus.

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- [1] E. E. Berlovich and Yu. N. Novikov, *Izv. AN SSSR ser. fiz.* 31, No. 2, 1967.
- [2] S. G. Nilsson, *Kgl. Mat. Fys. Medd. Dan. Vid. Selsk.* 29, No.16, 1955.
- [3] B. Mottelson and S. G. Nilsson, *Kgl. Mat. Fys. Dan. Vid. Selsk. Skrif.* 1, No. 8, 1959.
- [4] E. Marshalek, L. W. Person, and R. K. Sheline, *Revs. Modern Phys.* 35, 108 (1963).
- [5] E. E. Berlovich and Yu. N. Novikov, Abstracts, XV Conf. on Nucl. Spectroscopy and Nuclear Structure in Minsk, Nauka, 1965.
- [6] A. Sobiczewski, JINR Preprint E-2663, Dubna, 1966.
- [7] D. Bes and Z. Szymanski, *Nucl. Phys.* 28, 42 (1961); Z. Szymanski, *ibid.* 28, 63 (1961).
- [8] E. E. Berlovich, *JETP Letters* 4, 481 (1966), transl. p.323.
- [9] E. E. Berlovich, *Izv. AN SSSR ser. fiz.* 29, 2177 (1965), transl. Bull. Acad. Sci. Phys. Ser. p. 2013.
- [10] E. E. Berlovich, Preprint No. 007, Ioffe Physico-technical Inst. Leningrad, January 1967.