

CASCADE IONIZATION OF GAS IN A HIGH-INTENSITY LIGHT FIELD

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1. The Zel'dovich and Raizer theory of optical gas breakdown under the influence of laser emission [1] corresponds to the condition of relatively low rate of energy accumulation by the electron in the field of the electromagnetic wave:

$$\epsilon_0 \sigma_{tr} < I \sigma_i. \quad (1)$$

Here  $\epsilon_0 = e^2 E^2 / 2m\omega^2$  is the effective oscillation energy of an electron with charge  $e$  and mass  $m$  in the field of a wave with amplitude  $E_0$  and frequency  $\omega$ , and  $\sigma_{tr}$  and  $\sigma_i$  are respectively the transport cross section of elastic electron-atom collisions and the ionization cross section of atoms with ionization potential  $I$ . When the pulse duration  $T$  is decreased, the threshold flux density  $q = cE_0^2/8\pi$  in the theory [1] increases in proportion to  $1/T$ . Thus, condition (1) is violated if the pulse duration is sufficiently small.

If

$$\eta = \frac{\epsilon_0 \sigma_{tr}}{I \sigma_i} > 1 \quad (2)$$

the picture of the breakdown is radically altered.

When inequality (2) is satisfied, the electrons acquire during the time between two inelastic collisions an energy  $\epsilon$  greatly in excess of the ionization potential  $I$ . This means that in the energy space the trajectory of the electron produced as a result of the inelastic collision is determined by the formula

$$\frac{d\epsilon}{dt} = a(\epsilon), \quad (3)$$

where  $a(\epsilon) = \epsilon_0 N_0 \sigma_{tr}(\tau) v$ ,  $v$  is the electron velocity, and  $N_0$  is the atom density.

Assuming that the electrons produced as a result of the ionization have an initial energy  $\epsilon \ll \epsilon_0$ , we can write for the distribution function  $f(\epsilon, t)$ , at  $\epsilon > \epsilon_0$ , the kinetic equation

$$\frac{\partial f}{\partial t} + \frac{\partial}{\partial \epsilon} (a(\epsilon) f) = 0. \quad (4)$$

The solution of (4) is conveniently written in the form

$$f(\epsilon, t) = \frac{a(\epsilon(\tau_0))}{a(\epsilon)} F\left(t - \int_0^\epsilon \frac{d\epsilon'}{a(\epsilon')}\right), \quad (5)$$

where  $F(\tau)$  is an arbitrary function of  $\tau = t - \int_0^\epsilon d\epsilon'/a(\epsilon') \geq 0$ ,  $\tau_0$  is the time of ionization of the atom by an electron with zero initial energy, and  $\epsilon(\tau_0)$  is the energy acquired by the electron within the time  $\tau_0$ .  $F(\tau)$  can be determined from an integral equation corresponding

to the cascade-development model assumed by us:

$$F(r) = \int_0^{\epsilon(r)} F(r - \int_0^{\epsilon'} \frac{d\epsilon'}{\alpha(\epsilon')}) N_0 \sigma_i(\epsilon) v \frac{d\epsilon}{\alpha(\epsilon)}. \quad (6)$$

Indeed, equating the number of electrons in the energy interval from  $\epsilon$  to  $\epsilon + d\epsilon$  at the instant of time  $t$  to the number of electrons produced as a result of ionization during the time interval from  $\tau + d\tau$  to  $\tau$ , we obtain (6). The solution (6) can be represented in the form

$$F(\tau) = F_0 e^{\gamma\tau}, \quad (7)$$

where  $F_0 = n_0/\tau_0 \alpha(\epsilon(\tau_0))$  is a normalization function that takes into account the contribution of the bare electrons  $n_0$  to  $f$ . Substituting (7) in (6) and setting the upper limit of integration equal to infinity, we obtain an equation for the cascade-development constant  $\gamma$ :

$$N_0 \sqrt{\frac{2}{m}} \int_0^{\infty} \exp\left\{-\gamma \int_0^{\epsilon'} \frac{d\epsilon'}{\alpha(\epsilon')}\right\} \frac{\sigma(\epsilon) \sqrt{\epsilon} d\epsilon}{\alpha(\epsilon)} = 1. \quad (8)$$

In particular, when  $\alpha(\epsilon)$  is constant and  $\sigma_i$  decreases at high energies like  $1/\epsilon$  [2], the electron density  $n(t) = \int_0^{\infty} f(\epsilon, t) d\epsilon$ , the average electron energy  $\bar{\epsilon}(t) = 1/n(t) \int_0^{\infty} f(\epsilon, t) \epsilon d\epsilon$ , and the laser-emission absorption coefficient  $k(t)$  are respectively equal to

$$n(t) = \frac{n_0}{r_0 \gamma} e^{\gamma t}, \quad \bar{\epsilon}(t) = \frac{\alpha}{\gamma}, \quad k(t) = \frac{\alpha n_0}{q \gamma r_0} e^{\gamma t}, \quad (9)$$

and the cascade-development constant  $\gamma$  is connected with the quantity  $\alpha$ , with the neutral-atom concentration  $N_0$ , and with the maximum ionization cross section  $\sigma_{im} = \sigma_i(\epsilon_m)$  by the relation

$$\gamma = \frac{2\pi}{\alpha m} N_0^2 \epsilon_m^2 \sigma_{im}^2. \quad (10)$$

In the indicated case, the cascade-development time  $\theta = 1/\gamma$  is proportional to the radiation flux density  $q$ , the electron concentration at a fixed value of the time decreases with increasing  $q$ , and the average electron energy does not depend on the time and increases in proportion to  $q^2$ .

The applicability of this mechanism of ionization is limited from below by the condition (1), and from above by the photoionization in the strong field [3]. For example, for a neodymium laser pulse with  $T = 5 \times 10^{-12}$  sec,  $N_0 = 10^{19} \text{ cm}^{-3}$ , and  $I = 20$  eV the flux-density range amounts to  $\sigma_i/\sigma_{tr} 10^{14} < q < 10^{15} \text{ W/cm}$ .

[1] Ya. B. Zel'dovich and Yu. P. Raizer, Zh. Eksp. Teor. Fiz. 47, 1150 (1964) [Sov. Phys.-JETP 20, 772 (1965)].

[2] L. D. Landau and E. M. Lifshitz, Kvantovaya mekhanika, Fizmatgiz, 2d ed. 1963 [Quantum Mechanics, Addison-Wesley, 1958].