

transformation. Thus, the plot of the rate of nucleation against  $\Delta\mu$  should have two branches corresponding to the formation of a relaxed (partially coherent) phase<sup>4</sup>). Since the rate of nucleation is proportional to  $\exp(-F^*/kT)$ , it follows that the rate of nucleation during the formation of a low-temperature phase from a high-temperature one should be nonmonotonic (Fig. b).

The absolute values of the rates of nucleation of coherent and partly-coherent phases may differ significantly. For example, at small  $\Delta\mu$ , when  $\tau^* \gg r_c$  and  $\rho^* \approx \epsilon_0/b$ ,  $F^* = (16\pi/3)(\sigma^0 + \alpha G b \epsilon_0)^3 / \Gamma \mu^2$  and, if  $\sigma^0 < \alpha G b \epsilon_0$ , the rate of nucleation of the relaxed phase is lower by several orders of magnitude than the rate of coherent nucleation at equal values of the moving force. It is necessary to add to the already noted difference between the barriers to nucleation also the difference between the mobilities of the interphase boundaries [1], which makes the rate of transition with formation of a coherent phase much larger than for the transition with formation of a relaxed phase. The formation of a coherent or partly coherent phase corresponds apparently to two known kinetic types of transition in a single-component system, viz., normal and martensitic [2].

- [1] A.L. Roitburg, ZhETF Pis. Red. 13, 95 (1971) [JETP Lett. 13, 66 (1971)].  
 [2] G.V. Kurdyumov, Problemy metallovedeniya i fiziki metallov (Problems of Metallography and Metal Physics), M., Vol. 3, 9 (1952).

$\rho^0 - \omega$  INTERFERENCE IN THE REACTIONS  $\gamma N \rightarrow \pi^+ \pi^- \Delta$

N.N. Achasov and G.N. Shestakov  
 Mathematics Institute, Siberian Division, USSR Academy of Sciences  
 Submitted 18 February 1972  
 ZhETF Pis. Red. 15, No. 7, 427 - 430 (5 April 1972)

1. At the present time, the main information concerning the magnitude and phase of the  $\omega \rightarrow \pi^+ \pi^-$  decay due to electromagnetic  $\rho^0 - \omega$  mixing [1 - 3] is obtained from experiments on the study of the effects of  $\rho^0 - \omega$  interference in  $\pi^+ \pi^-$  mass spectra [4 - 6]. For a quantitative determination of the parameters of the electromagnetic  $\rho^0 - \omega$  mixing it is important to know the relative magnitude, the relative phase, and the degree of coherence of the amplitudes of  $\rho^0$ - and  $\omega$ -meson production reactions. Therefore reactions with known simple mechanisms of  $\rho^0$  and  $\omega$  production are most convenient for the study of the  $\rho^0 - \omega$  mixing.

At the same time, the  $\rho^0 - \omega$  interference in the  $\pi^+ \pi^-$  system can be used to verify and refine the theoretical mechanisms of  $\rho^0$  and  $\omega$  production [4].

In both cases, special interest attaches to processes in which the cross sections for  $\omega$ -meson production are much larger than  $\rho^0$ -production cross sections, since it is necessary to expect for them a considerable enhancement of the  $\rho^0 - \omega$  interference.

We wish to note in the present article that examples of such reactions are the reactions  $\gamma N \rightarrow \rho^0 \Sigma$  and  $\gamma N \rightarrow \omega \Delta$ , experiments on which are being performed at present and for which the first data have already been obtained [7 - 12].

<sup>4</sup>) If the relaxation takes place with participation of more than one type of dislocation, then their sequential inclusion in the process may become manifest by the appearance of new kinetic branches of the transformation.

We shall show that theoretical considerations lead us to expect in the reactions  $\gamma N \rightarrow \pi^+\pi^-\Delta$  a much stronger  $\rho^0 - \omega$  interference effect than in the well-studied reactions  $\gamma A \rightarrow \pi^+\pi^-A$  (see the figure).

2. The mass spectrum of the  $\pi^+\pi^-$  mesons with allowance for  $\rho^0 - \omega$  mixing in the resonance region is written in the form (cf., e.g., [4]):

$$\frac{dN(\pi^+\pi^-)}{dm} \sim \frac{N_\rho \Gamma_\rho}{|D_\rho(m)|^2} \left( 1 + 2d \cos \phi \left| \frac{\delta}{D_\omega(m)} \right| \frac{N_\omega^{1/2}}{N_\rho^{1/2}} + \frac{N_\omega}{N_\rho} \left| \frac{\delta}{D_\omega(m)} \right|^2 \right). \quad (1)$$

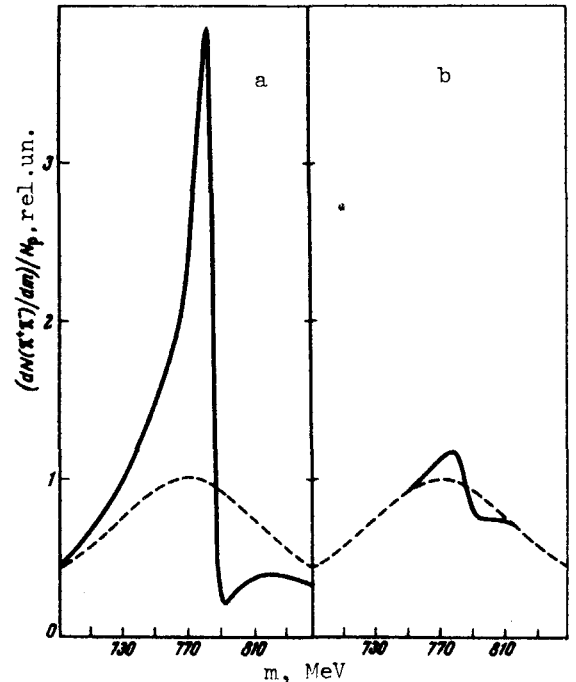
Here  $m$  is the invariant mass of the  $\pi^+\pi^-$  system,  $N_V$  is the total number of  $V$ -meson production events ( $V = \rho^0, \omega$ ),  $D_V(m) = m - m_V + i\Gamma_V/2$ ,  $m_V$  and  $\Gamma_V$  are respectively the mass and width of the  $V$  meson, and  $\delta$  is the amplitude of the electromagnetic  $\rho^0 - \omega$  transition. The coherence factor  $d$  and the phase  $\phi$  are given by

$$d = \left| \frac{\sum_i A_i^\rho A_i^\omega}{\left[ \left( \sum_i |A_i^\rho|^2 \right) \left( \sum_i |A_i^\omega|^2 \right) \right]^{1/2}} \right|; \quad (2)$$

$$\phi = \phi_\delta + \arctg \frac{\Gamma_\omega}{2(m_\omega - m)} + \arctg \frac{\sum_i |A_i^\rho| |A_i^\omega| \sin \phi_i}{\sum_i |A_i^\rho| |A_i^\omega| \cos \phi_i},$$

where  $A_i^V$  is the amplitude for the production of a  $V$  meson with definite spin configuration of the particles that take part in the reaction,  $\phi_\delta$  is the phase of  $\delta$ , and  $\phi_i$  is the relative phase shift between the amplitudes  $A_i^\rho$  and  $A_i^\omega$ .

To see that  $\rho^0 - \omega$  interference effect can be expected in the reactions  $\gamma N \rightarrow \pi^+\pi^-\Delta$  at high energies, let us attempt to establish the relative values and relative phase shifts of the  $\rho^0\Delta$  and  $\omega\Delta$  photoproduction amplitudes. To this end let us consider the mechanisms of the processes  $\gamma N \rightarrow \rho^0\Delta$  and  $\gamma N \rightarrow \omega\Delta$ . The  $\gamma N \rightarrow \omega\Delta$  amplitudes are due to the exchange of the following quantum numbers in the  $t$ -channel: the isotopic spin  $I = 1$ , the charge parity  $C = +1$ , and the parity  $P = \pm 1$ . In the  $\gamma N \rightarrow \rho^0\Delta$  reaction, besides the exchanges of the same quantum numbers in the  $t$ -channel, the exchange  $I = 2$  is also possible. In addition, the interference between the amplitudes with  $I = 2$  and  $I = 1$  can be excluded by considering the sum of the cross sections of the reactions  $\gamma p \rightarrow \rho^0\Delta^0$  and  $\gamma n \rightarrow \rho^0\Delta^0$ . We shall henceforth neglect the exchange  $I = 2$  in the  $t$ -channel. Then the mechanisms of the  $\rho^0\Delta$  and  $\omega\Delta$  photoproduction will be due to exchange of fully identical  $t$ -channel quantum numbers. We assume furthermore that at high energies the intermediate states of the  $t$ -channel of the  $\gamma N \rightarrow V\Delta$  reactions are only  $SU(3)$  octets, which is valid, for example, the Regge-pole model and in the model of poles with absorption. Applying now  $SU(3)$  symmetry to the  $t$ -channel amplitudes of the  $\gamma N \rightarrow V\Delta$  reactions,



$\rho^0 - \omega$  interference in the following reactions: a)  $\gamma N \rightarrow \pi^+\pi^-\Delta$ , b)  $\gamma A \rightarrow \pi^+\pi^-A$ .  $\Gamma_\rho = 140$  MeV,  $m_\rho = 770$  MeV,  $\Gamma_\omega = 12$  MeV,  $m_\omega = 784$  MeV,  $\delta = 2.9$  MeV.

we obtain the relation

$$A_i^{\rho}(\gamma N \rightarrow \rho^0 \Delta) \approx \frac{1}{3} A_i^{\omega}(\gamma N \rightarrow \omega \Delta). \quad (3)$$

We have used here also the fact that the sine of the mixing angle of the  $\omega$  and  $\phi$  mesons is equal to  $1/\sqrt{3}$ , and have neglected the amplitudes of the  $\gamma N \rightarrow \phi \Delta$  reaction, since the  $\phi$  meson is practically not connected with nonstrange particles<sup>1)</sup>. Consequently,

$$N_{\omega} \approx 9N_{\rho}, \quad d = 1, \quad \phi = \phi_{\delta} + \arctg \frac{\Gamma_{\omega}}{2(m_{\omega} - m)}. \quad (4)$$

The available experimental data on  $\rho^0 - \omega$  interference in  $\pi^+\pi^-$  mass spectra indicate that  $\delta$  is practically pure real, and  $\Gamma_{\omega 2\pi}/\Gamma_{\omega 3\pi} \approx 1 - 4\%$ , cf., e.g., [4 - 6], in accord with the theoretical estimates [1 - 3]. The continuous curve of Fig. a is a plot of the quantity  $(dN(\pi^+\pi^-)/dm)/N_{\rho}$  for the reactions  $\gamma N \rightarrow \pi^+\pi^-\Delta$ , calculated from formula (1) with allowance for (3) and the value  $\delta = 2.9$  MeV, corresponding to  $\Gamma_{\omega 2\pi}/\Gamma_{\omega 3\pi} \approx 2\%$ , ( $\Gamma_{\omega 2\pi} \approx 4|\delta|^2/\Gamma_{\rho}$ ), while the dashed line corresponds only to the  $\rho^0$  meson. Figure b shows the same for the reactions  $\gamma A \rightarrow \pi^+\pi^-A$ , and it is assumed here, as usual, that the main factor is the exchange of vacuum quantum numbers and the following relation is satisfied (cf., e.g., [4, 5]):

$$A_i^{\rho}(\gamma A \rightarrow \rho^0 A) \approx 3A_i^{\omega}(\gamma A \rightarrow \omega A). \quad (5)$$

As seen from (3) and (5), the interference term in (1) for  $\gamma N \rightarrow \pi^+\pi^-\Delta$  is enhanced by a factor 9 compared with the interference term for  $\gamma A \rightarrow \pi^+\pi^-A$ . This is also indicated by the presented diagrams.

3. In the study of quasi-two-particle reactions there arises the general question of separating the nonresonant background processes. In this case, the principal ones among them are apparently the processes  $\gamma p \rightarrow (\rho^0, \omega)\pi^+n$  and  $\gamma n \rightarrow (\rho^0, \omega)\pi^-p$ , which are large at high energies and are nonresonant in the region of  $\Delta$ , and in which the  $\pi N$  system is in a state with  $I = 1/2$ , while exchange of vacuum quantum numbers takes place in the  $t$ -channel. Their admixture may, in principle, smooth out the described picture of the  $\rho^0 - \omega$  interference in the reactions  $\gamma N \rightarrow \pi^+\pi^-\Delta \rightarrow \pi^+\pi^-(\pi N)$ , since relation (5) is satisfied for the amplitudes of such nonresonant reactions. If we take in the region of the  $\Delta$ -resonance the sum of the cross sections of the processes  $\gamma p \rightarrow \pi^+\pi^-(\pi^+n)$  and  $\gamma n \rightarrow \pi^+\pi^-(\pi^-p)$ , then the interference with the indicated background vanishes and it can be separated as incoherent.

We are grateful to I.F. Ginzburg, V.G. Serbo, V.V. Serebryakov, and V.L. Chernyak for a discussion and to D.V. Shirkov for interest in the work.

- [1] S.L. Glashow, Phys. Rev. Lett. 7, 469 (1961).
- [2] M. Gourdin, L. Stodolsky, and F.M. Renard, Phys. Lett. 30B, 347 (1969).
- [3] G.R. Allcock, Nucl. Phys. B21, 269 (1970).
- [4] G. Goldhaber, Talk presented at the 1970 Conference on Meson Spectroscopy Philadelphia, May 1 - 2, 1970; Preprint UCRL-19850.

<sup>1)</sup>We note that for one-pion exchange, which can predominate in a definite region of energies and momentum transfers [9, 10], and also for exchanges of  $A_1$  and  $A_2$  Regge poles in the vector-dominance model (VDM), we can obtain (for each of them) relation (3) accurate to within the phase. On the other hand, relation (3) is obtained within the VDM framework as a result of crossing symmetry for the vector mesons, which arises only in the SU(3) scheme.

- [5] R. Marshall, Talk presented at the International Conference on Meson Resonance and Related Electromagnetic Phenomena, Bologna, 14 - 16 April 1971; Preprint DNPL/P-73.
- [6] J. Lefrancois. Report presented at the 1971 International Symposium on Electron and Photon Interactions at High Energies, Ithaca, New York, Aug. 23 - 27, 1971; Preprint LAL-1256.
- [7] ABBHHM Collaboration, Phys. Rev. 188, 2060 (1969).
- [8] J. Ballam, et al., Phys. Lett. 30B, 421 (1969).
- [9] Y. Eisenberg, et al., Phys. Rev. Lett. 25, 764 (1970).
- [10] Y. Eisenberg, et al., Nucl. Phys. B25, 499 (1971).
- [11] J. Balam, et al., Phys. Rev. Lett. 26, 995 (1971).
- [12] A. Levy, SLAC Report No. 136, p. 9, September 1971.

QUANTUM NUMBERS AND TOTAL AND PARTIAL WIDTHS OF THE RESONANCE  $N\bar{N}$ (1970)

O.D. Dal'karov, B.O. Kerbikov, and I.S. Shapiro  
 Institute of Theoretical and Experimental Physics, USSR Academy of Science  
 Submitted 18 February 1972  
 ZhETF Pis. Red. 15, No. 7, 430 - 434 (5 April 1972)

We have previously considered [1] the resonant states in the nucleon-anti-nucleon system. A characteristic feature of these resonances is the large partial width of the decay through the nucleon-antinucleon channel. Calculations show that for resonances consisting of a nucleon and an antinucleon, the partial width  $\Gamma_{N\bar{N}}$  is of the same order of magnitude as the total width  $\Gamma$  [1]. For mesons of a different nature, in the same mass region, the  $N\bar{N}$  channel is not singled out in any way, and estimates based on the statistical theory yield  $\Gamma_{N\bar{N}}/\Gamma \sim 0.1 - 1\%$ .

In the present paper, on the basis of experimental data, we estimate the ratio  $\Gamma_{N\bar{N}}/\Gamma$  for the meson  $N\bar{N}$ (1970). This meson was observed in two independent experiments: in the reaction



and in elastic backward  $\bar{p}p$  scattering [2, 3]. In [2] they investigated the cross section of reaction (1) and the angular distribution of  $K_S^0 K_L^0$  at an incident-antiproton momentum lower than 800 MeV/c. The final state of  $K_S^0 K_L^0$  has negative C-parity (accurate to CP-violation, which is immaterial here). In the investigated region of incident antiproton momenta, the main contribution to the cross section of process (1) is made by the initial states of the  $\bar{p}p$  system with orbital angular momentum  $l$  not larger than two [4]. From C- and P-parity conservation it follows that at  $l \leq 2$  only the  $^3S_1$ ,  $^3D_1$ , and  $^3D_3$  states of the  $\bar{p}p$  system can participate in the reaction (1).

As was established in [2], the cross section of the process (1) has a clearly pronounced resonant character with a maximum in the 600 MeV/c region, corresponding to a resonance mass equal to 1970 MeV. The maximum value of the cross section in the resonant region exceeds by 3 - 4 times the background level. Therefore the cross section  $\sigma$  of reaction (1) can be represented in the form of an incoherent superposition of the smooth background  $\sigma^0$  and the Briet-Wigner resonance. At resonance we obtain the following expression for the sought ratio  $\Gamma_{N\bar{N}}/\Gamma$ :

$$\frac{\Gamma_{N\bar{N}}}{\Gamma} = \left( \frac{\Gamma}{\Gamma_{K_S^0 K_L^0}} \right) \frac{(\sigma - \sigma_0) p^2}{\pi (2l + 1)}, \quad (2)$$