Quasi-one-dimensional quantum spin liquid in the $Cu(C_4H_4N_2)(NO_3)_2$ insulator

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We analyze measurements of the magnetization, differential susceptibility and specific heat of quasi-one dimensional insulator $Cu(C_4H_4N_2)(NO_3)_2$ (CuPzN) subjected to magnetic fields. We show that the thermodynamic properties are defined by quantum spin liquid formed with spinons, with the magnetic field tuning the insulator CuPzN towards quantum critical point related to fermion condensation quantum phase transition (FCQPT) at which the spinon effective mass diverges kinematically. We show that the FCQPT concept permits to reveal and explain the scaling behavior of thermodynamic characteristics. For the first time, we construct the schematic T-H (temperature–magnetic field) phase diagram of CuPzN, that contains Landau–Fermi-liquid, crossover and non-Fermi liquid parts, thus resembling that of heavy-fermion compounds.

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Recently, the striking measurements of the thermodynamic properties at low temperatures T under the application of magnetic field H on the quasi-one dimensional (Q1D) insulator $Cu(C_4H_4N_2)(NO_3)_2$ (CuPzN) have been performed [1]. The observed thermodynamic properties of CuPzN is very unusual and nobody expects that it might belong to the class of HF compounds, including quasicrystals (QC) [2], insulators with quantum spin liquid (QSL), and heavy-fermion (HF) metals [3– 6]. Similar Q1D clean HF metal YbNi₄ P_2 was recently experimentally studied, that reveals it has a Q1D electronic structure and strong correlation effects dominating the low-temperature properties, while its thermodynamic properties resembles those of HF metals, including the formation of Landau–Fermi-liquid (LFL) ground state [7]. These observations show that both CuPzN and YbNi₄P₂ can demonstrate a new type of Q1D Fermi liquid whose thermodynamic properties resemble that of HF compounds rather than the Tomonaga–Luttinger system. One of the hallmark features of geometrically frustrated insulators is spin-charge separation. The behavior of Q1D Fermi liquid (Q1DFL) is the subject of ongoing intensive experimental research in condensed

matter physics, see, e.g., [1] and references therein. Q1DFL survives up to the saturation magnetic field H_s , where the quantum critical point (QCP) occurs giving way to a gapped, field-induced paramagnetic phase [1]. In other words, at $H = H_s$ both antiferromagnetic (AFM) sublattices align in the field direction i.e. the magnetic field fully polarizes Q1DFL spins. We will see below that in Q1DFL the fermion condensation quantum phase transition (FCQPT) plays a role of QCP, at which the energy band for spinons becomes almost flat at $H = H_s$ and the effective mass M^* of spinons diverges due to kinematic mechanism. Thus, the bare interaction of spinons is weak [1]. In that case the original Tomonaga–Luttinger system can exactly be mapped on a system of free spinons, which low-temperature behavior in magnetic fields can be viewed as the LFL one [8]. Thus CuPzN offers a unique possibility to observe a new type of Q1D QSL whose thermodynamic properties resemble that of HF compounds like HF metals, including Q1D HF metal YbNi₄P₂ [7], quantum spin liquids of herbertsmithite $ZnCu_3(OH)_6Cl_2$ [6], and liquid ³He [9]. Theory of Q1D liquids is still under construction and recent results show that the liquids can exhibit LFL, non-Fermi liquid (NFL) and crossover behavior [8, 10, 11].

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In this letter we show that, contrary to ordinary wisdom, CuPzN can be regarded as an insulator belonging to HF compounds, while its thermodynamic properties are defined by weakly interacting Q1D QSL formed with spinons, and are similar to those of HF compounds. Here spinons are chargeless fermionic quasiparticles with spin 1/2. For the first time, we demonstrate that its T-Hphase diagram contains LFL, crossover and NFL parts, thus resembling that of HF compounds. To unveil the relation between CuPzN and HF compounds, we study the scaling behavior of its thermodynamic properties which are independent of the interparticle interaction. We demonstrate that CuPzN exhibits the universal scaling behavior, that is typical of HF compounds.

Upon transition to fermionic description, CuPzN is indeed represented by weakly interacting fermions. The description of weakly interacting fermion gas gives magnetization in terms of fermion number per spin N/L = $= \int_0^\infty D(\varepsilon) f[\varepsilon - \mu(H)] d\varepsilon$, where L is the number of spins in Q1D chain, $D(\varepsilon)$ is the density of states, corresponding to free fermion spectrum $\varepsilon = p^2/(2m_0)$ with p is the momentum and m_0 is the bare mass. The chemical potential $\mu(H) = H_s - H$, and $f(x) = (e^x + 1)^{-1}$ is the Fermi distribution function [1, 12, 13]. The magnetization can be expressed as $M = M_s - N$ (M_s is the saturation magnetization) or explicitly

$$M(H,T) = M_s - \frac{\sqrt{2m_0T}}{\pi} \int_0^\infty \frac{dx}{e^{\left(x^2 - \frac{H_s - H}{T}\right)} + 1}.$$
 (1)

Eq. (1) will be used below to calculate the differential magnetic susceptibility $\chi(T, H) = \frac{\partial M(T, H)}{\partial H}$. To calculate the specific heat C(T, H), we need the internal energy E, which in the above approach can be calculated as follows

$$E(T,H) = \int_0^\infty \varepsilon D(\varepsilon) f[\varepsilon - \mu(H)] d\varepsilon, \qquad (2)$$

so that $C(T, H) = \frac{\partial E}{\partial T}$. Within the framework of fermionic description, as it is seen from Eq. (1), CuPzN is indeed a weakly interacting fermions with simplest possible spectrum $\varepsilon = p^2/(2m_0)$, where (in atomic units) $\hbar = c = 1$. Near QCP taking place at $H = H_s$ and T = 0, the fermion spectrum becomes almost flat, and the fermion (spinon) effective mass diverges, $M^* \propto m_0/p_{\rm F} \to \infty$, due to kinematic mechanism, for the Fermi momentum $p_{\rm FH} \to 0$ of becoming empty subband. In case of weak repulsion between spinons the divergence is associated with the onset of a topological transition at finite value of $p_{\rm FH}$ signaling that $M^*(T) \propto \propto T^{-1/2}$ [3, 14–17]. In accordance with Ref. [8], we suggest that the weakly interacting Q1DFL in CuPzN could be thought of as QSL, formed with fermionic spinons, constituting the Fermi sphere (line) with the Fermi momentum $p_{\rm F}$, and carrying spin 1/2 and no charge. For QCP occurs at $M^* \to \infty$, as we have seen above, we propose that QCP is FCQPT, at which the corresponding band becomes approximately flat [3–6].

In fermion representation the ground state energy E(n) can be viewed as the Landau functional depending on the spinon distribution function $n_{\sigma}(\mathbf{p})$, where \mathbf{p} is the momentum. Near FCQPT point, the effective mass M^* is governed by the Landau equation [18, 4, 5]

$$\frac{1}{M^*(T,H)} = \frac{1}{M^*(T=0,H=0)} + \frac{1}{p_F^2} \sum_{\sigma_1} \int \frac{\mathbf{p}_F \mathbf{p}_1}{p_F} F_{\sigma,\sigma_1}(\mathbf{p}_F,\mathbf{p}_1) \frac{\partial \delta n_{\sigma_1}(\mathbf{p}_1)}{\partial p_1} dv, \quad (3)$$

where dv is the volume element. Here we have rewritten the spinon distribution function as $\delta n_{\sigma}(\mathbf{p}) \equiv$ $\equiv n_{\sigma}(\mathbf{p}, T, B) - n_{\sigma}(\mathbf{p}, T = 0, B = 0)$. The sole role of the Landau interaction $F(\mathbf{p}_1, \mathbf{p}_2) = \delta^2 E / \delta n(\mathbf{p}_1) \delta n(\mathbf{p}_2)$ is to bring the system to FCQPT point, where $M^* \to \infty$ at T = 0, and the Fermi surface alters its topology so that the effective mass acquires temperature and field dependences, while the proportionality of the specific heat C/T and the magnetic susceptibility χ to M^* holds: $C/T \sim \chi \sim M^*(T, H)$ [4, 5, 19, 20]. This feature can be used to separate the solutions of Eq. (3), corresponding to specific experimental situation. Namely, the experiment on CuPzN shows that near QCP at $H = H_s$, the specific heat $C(T)/T \propto \chi(T) \propto T^{-1/2}$ [1] which means that M^* is responsible for the observed behavior, while QCP is formed by kinematic mechanism. It has been shown that near FCQPT, $M^*(T) \propto T^{-1/2}$, while the application of H drives the system to the LFL region with $M^{*}(H) \propto (H_{s} - H)^{-1/2}$ [4, 5, 3]. At finite H and T near FCQPT, the solutions of Eq. (3) $M^*(T, H)$ can be well approximated by a simple universal interpolating function [4, 3, 5]. The interpolation occurs between the LFL $(M^* \propto a + bT^2)$ and NFL $(M^* \propto T^{-1/2})$ regimes and represents the universal scaling behavior of $M_N^*(T_N)$ independent of spatial dimension of the considered system

$$M_N^* = \frac{1+c_2}{1+c_1} \frac{1+c_1 T_N^2}{1+c_2 T_N^{5/2}},\tag{4}$$

where c_1 and c_2 are fitting parameters, $M_N^* = M^*/M_M^*$ and $T_N = T/T_M$ are the normalized effective mass and temperature respectively. Here,

$$M_M^* \propto (H_s - H)^{-1/2},$$
 (5)

$$T_M \propto H_s - H \tag{6}$$

are the maximum value of the effective mass M_M^* and temperature T_M , corresponding to the maximum of $(dM/dT)_{\max}(H)$ and/or $\chi_{\max}(H)$ [3, 4, 5]. Below Eq. (4) is used along with Eq. (1) to describe the experiment in CuPzN.

Taking into account that $M = \int \chi dH$ and Eqs. (4), (5), and (6), we obtain that $(M - M_s)/\sqrt{H_s - H}$ as a function of the variable $T/(H_s - H)$ exhibits scaling behavior. This result is in good agreement with the experimental facts, as it is seen from Fig. 1 that reports



Fig. 1. (Color online) The scaling behavior of the magnetization $M_c/B^{0.5}$ versus T/B at different magnetic fields H, shown in the legend, with $M_c = a + (M - M_s)$ and $B = H_s - H$. The LFL, crossover and NFL regions are shown by the arrows. The data are extracted from measurements [1]

the plot of the scaling behavior of the magnetization $M_c/B^{0.5} = a + (M - M_s)/(H_s - H)^{0.5}$ as a function of $T/B = T/(H_s - H)$, with *a* is a constant added to a better presentation of the Figure. It is seen from Fig. 1, that the LFL behavior takes place at $T \ll B$, the crossover at $T \sim B$, and the NFL one at $T \gg B$, as it is in the case of HF compounds [4, 5]. It is instructive to note that the same scaling behavior exhibits M_c obtained in measurements on YbAlB₄ under the application of magnetic field [21], see Fig. 1b of Ref. [22].

Fig. 2 portrays the comparison between χ_N extracted from the experiments on CuPzN (panel a) [1], Au₅₁Al₃₄Yb₁₅ quasicrystal (panel b) [23], and the theory. Here χ_N is the normalized magnetic susceptibility, while the normalization is done in the same way as it is done in the case of M_N^* [4, 5]. It is seen that for more then three decades in normalized temperature there is very good agreement between the theory and the experimental data. The double log scale, used in panels a and b, reveals the universal dependence $\chi_N \sim T_N^{-0.5}$.

The comparison between Fig. 2a and b indicates that χ_N of both CuPzN and the quasicrystal Au₅₁Al₃₄Yb₁₅ has three regions: low-temperature LFL part, mediumtemperature crossover region where the maximum occurs, and high-temperature NFL part with the distinctive temperature dependence $T_N^{-0.5}$. Note that the dependences from Figs. 2a and b qualitatively resemble that of Q1D HF metal YbNi₄ P_2 [7], and demonstrate the scaling behavior, and are similar to those of heavyfermion compounds [3, 5]. We recall that the absolute values of the thermodynamic functions obviously depend on the interparticle interaction amplitude, therefore, to reveal the universal properties we have to employ the normalization procedure [3–5]. We note, that the approach of weakly interacting Q1DFL (1) gives for C/T and χ the same high-temperature asymptotics $T^{-1/2}$.

Fig. 3a shows the normalized temperature dependence $(dM/dT)_N$ of the quantity dM/dT, revealing the scaling behavior, while the normalization is done in the same way as it is done in the case of M_N^* or χ_N . The black solid theoretical curve corresponds to the temperature derivative dM/dT of the magnetization (1). Good coincidence with experiment on CuPzN is seen everywhere. Such a good agreement shows that dM/dThas the universal scaling behavior, that can also be described by taking into account that $M = \int \chi dH$. In panel b of Fig. 3 the maximum values $(dM/dT)_{\rm max}$ of dM/dT versus $H_s - H$ are displayed. The theoretical curve given by $(dM/dT)_{\rm max} \propto (H_s - H)^{-1/2}$ is in good agreement with experimental facts extracted from measurement of the magnetization [1], and demonstrates that the effective mass of spinons does diverge at $H \to H_s$.

The above thermodynamic properties reported in Figs. 2, 3, and 4 coincide with those of HF compounds, and permit us to construct the T-H phase diagram of CuPzN, shown in Fig. 5. To do so, in Fig. 4a we report the peak temperature T_M of magnetic susceptibility as a function of H. It is seen, that the peak temperature T_M goes to zero as H approaches H_s . In panel b of Fig. 4 the maximum values $\chi_{\rm max}$ of χ versus $H_s - H$ are displayed. It is seen, that theoretical curve given by Eq. (5) is in good agreement with experimental data extracted from measurement of the magnetization [1], and demonstrates that the effective mass of spinons does diverge at $H \to H_s$, as it is at FCQPT. The T-H phase diagram reported in Fig. 5 demonstrates that peak dependence T_M takes place over wide range of variation of H, for $T_M \propto H_s - H$. This shows, that main property of these lines is that they are straight lines, representing energy scales typical for HF metals located at their



Fig. 2. (Color online) (a) – The normalized magnetic susceptibility χ_N extracted from measurements in magnetic fields H (shown in the legend) on CuPzN [1] and on Au₅₁Al₃₄Yb₁₅ quasicrystal [23]. Our theoretical curves, merged in the scale of the Figure and plotted on the base of Eqs. (1) and (4), are reported by the solid lines tracing the scaling behavior. Panels a and b show that dependence $\chi_N(T_N)$ for CuPzN and quasicrystal has three distinctive regions: LFL, crossover and NFL, where $\chi_N \sim T_N^{-0.5}$ shown by the straight line



Fig. 3. (Color online) (a) – The normalized $(dM/dT)_N$ extracted from measurements in magnetic fields on CuPzN [1]. Theoretical curve, based on Eq. (1) is also reported. (b) – The magnetic field dependence of the maximum values $(dM/dT)_{\text{max}}$ of dM/dT. The theoretical curve is given by $(dM/dT)_{\text{max}} \propto (H_s - H)^{-1/2}$, see Eq. (5)

QCP [24, 25]. Since FCQPT takes place at $H = H_s$, the phase diagram is almost symmetric with respect to the point $H = H_s$, and consists of the LFL, gapped Fermi liquid, crossover and NFL regions. The crossover

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Fig. 4. (Color online) (a) – The magnetic field dependence of peak temperature T_M of the magnetic susceptibility χ of CuPzN, gathered from experimental data [1]. The calculated straight line $T_M \propto H_s - H$ given by Eq. (6) demonstrates good agreement with the experimental data. (b) – The magnetic field dependence of the maximum values $\chi_{\max}(H)$. The theoretical curve is given by $\chi_{\max} \propto (H_s - H)^{-1/2}$, see Eq. (5)

regions in Fig. 5 are shown by arrows, and are formed by the straight lines, which are the magnetic field dependencies of temperatures of approximate LFL and NFL boundaries as well as by that of T_M . NFL state occurs at relatively high temperatures with the distinct temperature dependence $\sim T_N^{-1/2}$. At the same time LFL regions occur at low T, where the spinon effective mass is almost constant, as is the case for LFL behavior. At $H > H_s$ the QSL becomes a gapped field-induced paramagnetic spin liquid, as shown in Fig. 5. At rising temperatures and fixed magnetic field H, the system transits through the crossover, and enters the NFL region, as it is seen from Fig. 5. It is also seen, that the crossover becomes wider, as the systems moves from FCQPT shown by the filled circle. We conclude that CuPzN exhibits the behavior typical for HF compounds [25] that leads to the formation of the corresponding T-H phase diagram displayed in Fig. 5.



Fig. 5. (Color online) Schematic magnetic field – temperature phase diagram of CuPzN, based on data from panels a of Fig. 2 for $H \leq H_s$. Straight lines on both sides of H_s , which is FCQPT point, indicate, respectively, the lines of LFL boundary (the lowest temperature), the temperatures of maxima (middle line, marked " T_M ") and the end of crossover region (the highest temperature at which the system enters the NFL regime), see Fig. 2a. The right sector labeled as "gapped FL" denotes the gapped fieldinduced paramagnetic spin liquid

In summary, we have shown that the thermodynamic properties of CuPzN are defined by weakly interacting QSL, and explained the corresponding experimental facts. Our analysis have shown that QCP, represented by FCQPT, in CuPzN occurs due to kinematic mechanism: The band becomes approximately flat not due to interaction between fermions but rather due to the application of sufficiently strong magnetic field $H = H_s$. We have constructed the T-H phase diagram of CuPzN and for the first time have shown that it is approximately symmetric with respect to QCP, and has the LFL part, crossover, gapped Fermi liquid, and NFL part. For the first time, we have also revealed that CuPzN exhibits the universal scaling behavior typical for HF compounds.

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